

1. Aplicar Carga "P"

$$\sum M_D = 0$$

$$C_y(3m) - 2 \text{ tn} \cdot m - P(3m) = 0$$

$$C_y = 2 \text{ tn} \cdot m / 3m - P(3m/3m)$$

$$C_y = 0.4 \text{ ton} - 0.6P$$

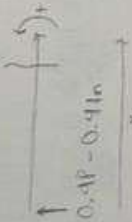
$$A_y - P + C_y = 0$$

$$A_y = P - (0.4 \text{ ton} - 0.6P)$$

$$A_y = 0.4P - 0.4 \text{ ton}$$

Corte 1

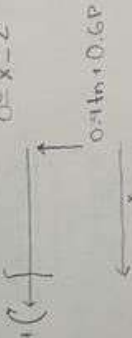
$$0 \leq x \leq 3$$



$$M_1 = 0.4P(x) - 0.4 \text{ ton}(x)$$

Corte 2

$$0 \leq x \leq 2$$



$$M_2 = 0.4 \text{ ton}(x) + 0.6P(x) - 2x$$

Determinar la deflexión en el Punto "E" de la viga.

$$M_1 = \frac{ap}{Z} = 0.4x$$

$$M_2 = \frac{ap}{Z} = 0.6x$$

Integral:

Formula

$$\Delta = \int_0^L \frac{M(x) \left( \frac{ap}{Z} \right) dx}{EI}$$

$$\Delta_{VE} = \int_0^3 \frac{(-0.4x)(0.4x) dx}{EI} + \int_0^2 \frac{(-0.16x^2) dx}{EI} + \int_0^2 \frac{(-0.16x^2) dx}{EI} + \int_0^2 \frac{(-0.053(x^2) - 0.053(x^2)) dx}{EI}$$

$$= \frac{1}{EI} \left[ -\frac{0.16x^3}{3} \right]_0^3 + \frac{1}{EI} \left[ -\frac{0.053x^3}{3} \right]_0^2 + \frac{1}{EI} \left[ -\frac{0.053x^3}{3} \right]_0^2 + \frac{1}{EI} \left[ -\frac{0.053x^3}{3} \right]_0^2$$

$$= \frac{1}{EI} \left[ -\frac{0.16(27)}{3} - \frac{0.053(8)}{3} - \frac{0.053(8)}{3} - \frac{0.053(8)}{3} \right] = -1.431$$

Integral

$$\Delta = \int_0^3 \frac{(-0.4x)(0.4x) dx}{EI} + \int_0^2 \frac{(-0.16x^2) dx}{EI} + \int_0^2 \frac{(-0.16x^2) dx}{EI} + \int_0^2 \frac{(-0.053(x^2) - 0.053(x^2)) dx}{EI}$$

$$\Delta_{VE} = \int_0^3 \frac{(-0.4x)(0.4x) dx}{EI} + \int_0^2 \frac{(-0.16x^2) dx}{EI} + \int_0^2 \frac{(-0.16x^2) dx}{EI} + \int_0^2 \frac{(-0.053(x^2) - 0.053(x^2)) dx}{EI}$$

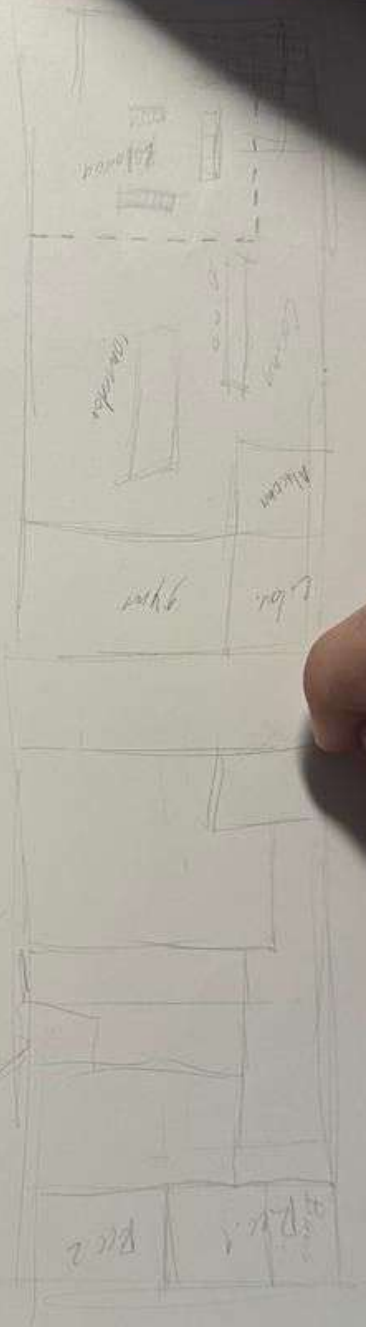
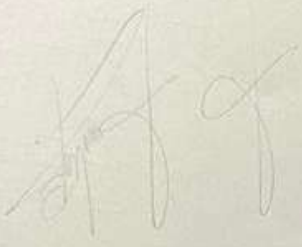
$$= \frac{1}{EI} \left[ -\frac{0.16x^3}{3} \right]_0^3 + \frac{1}{EI} \left[ -\frac{0.053x^3}{3} \right]_0^2 + \frac{1}{EI} \left[ -\frac{0.053x^3}{3} \right]_0^2 + \frac{1}{EI} \left[ -\frac{0.053x^3}{3} \right]_0^2$$

$$= \frac{1}{EI} \left[ -\frac{0.16(27)}{3} - \frac{0.053(8)}{3} - \frac{0.053(8)}{3} - \frac{0.053(8)}{3} \right] = -1.431$$

$$\Delta V = \int_0^2 \frac{(-2)(0.6x)}{EI} dx = \frac{1}{EI} \int_0^2 (-1.2x) dx = \frac{1}{EI} \left[ -0.6x^2 \right]_0^2 = \frac{-0.6 \cdot 4}{EI} = \frac{-2.4}{EI}$$

$$\frac{-0.4x^2}{EI} \int_0^2 \frac{-0.4(2)^2}{EI} = \frac{-0.4(4)}{EI} = \frac{-1.6}{EI}$$

$$-1.431 + 0.64 - 2.4 = -3.191$$



$$\frac{0.4x^2}{EI} \int_0^2 \frac{0.4(2)^2}{EI} = \frac{0.4(4)}{EI} = \frac{1.6}{EI}$$

$$\int_0^2 \frac{0.6x^2}{EI} = \frac{0.6x^3}{3EI} \Big|_0^2 = \frac{0.6 \cdot 8}{3EI} = \frac{1.6}{EI}$$