



Mi Universidad

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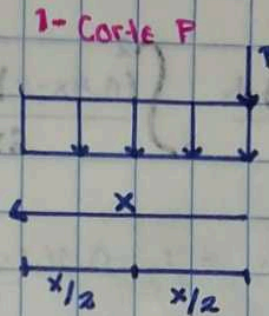
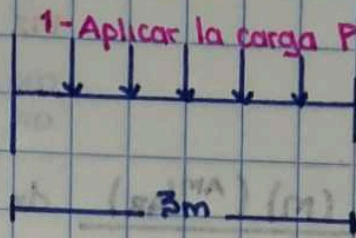
MATERIA: ANALISIS DE UNA ESTRUCTURA

TEMA: INESTABILIDAD ELASTICA

PARCIAL: 4TO

LICENCIATURA: LICENCIATURA EN ARQUITECTURA

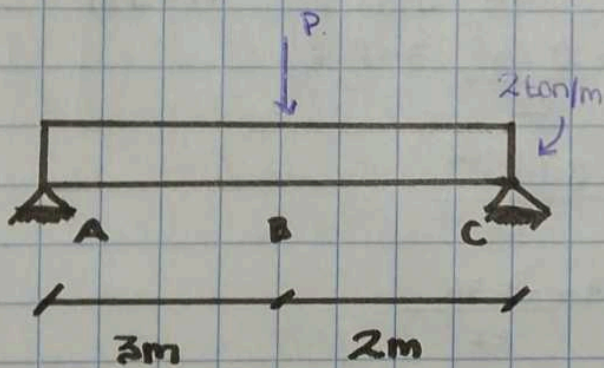
CUTRIMESTRE: 4TO



$$M = -P(x) - 2\left(\frac{x}{2}\right) \\ = -P(x) - x^2$$

$$\Delta_0 = \int_0^L \frac{(M) \left(\frac{\Delta M}{\Delta R}\right) dx}{EI} \\ \Delta_0 = \int_0^3 (x^2)(-x) dx$$

$$\frac{(3)^4}{4} - \frac{(0)^4}{4} = \frac{81}{4} = 20.25$$



Determinar la deflexión en el punto "B" de la viga

1- Aplicar la carga (P)

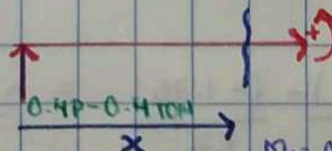
$$C_y(5m) - 2\text{ton/m} - P(3m) = 0 \\ C_y = \frac{2\text{ton}\cdot\text{m}}{5m} + P\left(\frac{3m}{5m}\right) \\ C_y = 0.4\text{ton} + 0.6P$$

$$A_y - P + C_y = 0 \\ A_y = P - (0.4\text{ton} - 0.6P) \\ A_y = 0.4P - 0.4\text{TON}$$

P=1

CORTE 1

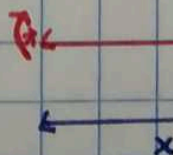
$$0 \leq x \leq 3$$



$$M_1 = 0.4P(x) - 0.4\text{ton}(x)$$

CORTE 2

$$0 \leq x \leq 2$$



$$0.4\text{ton} + 0.6P$$

$$M_2 = 0.4\text{ton}(x) + 0.6P(x) - 2$$

M1

$$\frac{QM}{QR} = 0.4x$$

M2

$$\frac{QM}{QR} = 0.6x$$

FORMULA

$$\Delta = \int_0^L \frac{(M) (AM/AR)}{EI} dx$$

$$\Delta = \int_0^3 \frac{(-0.4x)(0.4x)}{EI} dx + \int_0^2 \frac{(0.4x-2)(0.6x)}{EI} dx$$

$$\Delta = \int_0^3 (-0.16x^2) dx = \frac{1}{EI} \left[-0.16 \frac{(x^{n+1})}{n+1} \right]_0^3 = \frac{1}{EI} \left[\frac{0.16(x^{2+1})}{2+1} \right]_0^3 =$$

$$\frac{1}{EI} \left[\frac{-0.16x^3}{3} \right]_0^3 = \frac{1}{EI} \left[\frac{-0.053x^3}{EI} \right]_0^3 = \frac{-0.053x^3}{EI} \Big|_0^3 = \frac{-0.053(3)^3}{EI} = \frac{-1.431}{EI}$$

$$\frac{0.053(0)^3}{EI} = \frac{0.053(27)}{EI} = \frac{-1.431}{EI}$$

$$\Delta = \int_0^2 (0.24x^2 - 1.2x) dx = \frac{1}{EI} \left[\frac{0.24(x^{2+1})}{2+1} \right]_0^2 - \left[\frac{1.2(x^{1+1})}{1+1} \right]_0^2 =$$

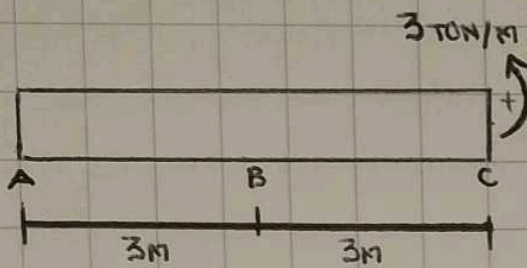
$$\frac{1}{EI} \frac{0.08x^3}{1} - \frac{1}{EI} \frac{0.6x^2}{1} = \frac{0.08x^3}{EI} - \frac{0.6x^2}{EI} = F-F$$

$$\frac{0.08(2)^3}{EI} - \frac{0.08(0)^3}{EI} - \frac{0.6(2)^2}{EI} - \frac{0.6(0)^2}{EI}$$

$$\frac{0.08(8)}{EI} - \frac{0.6(4)}{EI} = \frac{0.64}{EI} - \frac{2.4}{EI} = \frac{-1.76}{EI}$$

$$\Delta = \frac{(-1.431)}{EI} - \frac{(-1.76)}{EI} = \frac{-3.191}{EI} \uparrow$$

DETERMINAR LA DEFLEXIÓN EN EL CENTRO DE LA VIGA



1- Aplicar carga P

$$C_y(6m) + 3 \text{ ton/m} \cdot 6m + P(3m) = 0$$

$$C_y = +3 \text{ ton/m} / 6m + P(3m/6m)$$

$$C_y = +0.5 \text{ ton} + 0.5P$$

$$A_y - P + C_y = 0$$

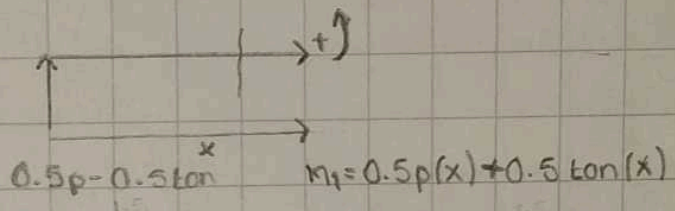
$$A_y = P - (0.5 \text{ ton} + 0.5P)$$

$$A_y = 0.5P - 0.5 \text{ ton}$$

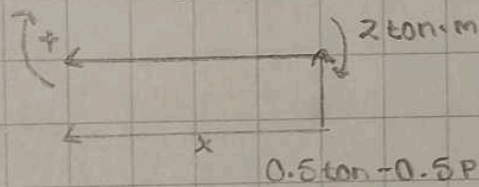
$$AM/AR = 0.5x \rightarrow M_1$$

$$AM/AR = 0.5x \rightarrow M_2$$

CORTE 1 $0 \leq x \leq 3$



CORTE 2 $0 \leq x \leq 3$



$$M_2 = 0.5 \text{ ton}(x) + 0.5P(x) + 3$$

FORMULA
$$\Delta = \int_0^L \frac{(M) (AM/AR)}{EI} dx$$

$$\Delta = \int_0^3 \frac{(0.5x)(0.5x)}{EI} dx$$

$$\Delta = \int_0^3 \frac{-0.25x^2}{EI} dx$$

$$\Delta = -0.25 \left(\frac{x^{2+1}}{2+1} \right) \Big|_0^3$$

$$\Delta = -\frac{0.25x^3}{3}$$

$$\Delta = -\frac{0.0833x^3}{IE}$$

$$\int_0^3 \frac{(-0.5x+3)(0.5x)}{EI} dx$$

$$\int_0^3 \frac{(0.25x^2 + 1.5x)}{EI} dx$$

$$\frac{0.25(x^{2+1})}{2+1} + \frac{1.5(x+1)}{1+1} \Big|_0^3$$

$$\frac{0.25x^3}{3} + \frac{1.5x^2}{2}$$

$$\frac{0.0833x^3}{IE} + \frac{0.75x^2}{IE}$$

Silky

$$\Delta = + \frac{0.0833(3)^3}{IE} + \frac{0.0833(3)^3}{IE} + \frac{0.75(3)^2}{IE}$$

$$\Delta = + \frac{0.0833(27)}{IE} + \frac{0.0833(27)}{IE} + \frac{0.75(9)}{IE}$$

$$\Delta = + \frac{2.2491}{EI} + \frac{2.2491}{EI} + \frac{6.75}{EI}$$

$$\Delta = \frac{6.75}{EI}$$