



Mi Universidad

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Nombre del tema: INESTABILIDAD ELASTICA

Unida: 4

Nombre de la Materia: ANALISIS DE ESTRUCTURAS

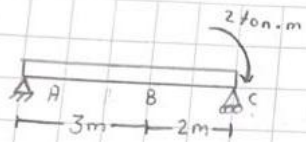
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Nombre de la Licenciatura: Arquitectura

Cuatrimestre: 5

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BOOK



Determinar la deflexión en el punto "B" de la viga

1. Aplicar carga "P"

$$\sum M_0 = 0$$

$$c_y (5m) - 2 \text{ ton. m} - P (3m) = 0$$

$$c_y = 2 \text{ ton. m} / 5m - P (3m) / 5m$$

$$c_y = 0.4 \text{ ton} - 0.6 P$$

$$A_y - P + c_y = 0$$

$$A_y = P - (0.4 \text{ ton} - 0.6 P)$$

$$A_y = 0.4 P - 0.4 \text{ ton}$$

CORTE 1

$$0 \leq x \leq 3$$

$$0.4 P - 0.4 \text{ ton} \quad M_1 = 0.4 P(x) - 0.4 \text{ ton}(x)$$

CORTE 2

$$0 \leq x \leq 2$$

$$0.4 \text{ ton} - 0.6 P \quad M_2 = 0.4 \text{ ton}(x) + 0.6 P(x) - 2$$

$\frac{\partial M}{\partial P} = 0.4x \rightarrow M_1$

$\frac{\partial M}{\partial P} = 0.6x \rightarrow M_2$

formula

$$\Delta = \int_0^3 \frac{(M) \left(\frac{\partial M}{\partial P} \right)}{EI} dx$$

$$\Delta = \int_0^3 \frac{(-0.4x)(0.4x)}{EI} dx + \int_0^2 \frac{(0.4x - 2)(0.6x)}{EI} dx$$

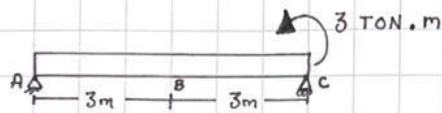
$$\Delta = \int_0^3 \frac{-0.16x^2}{EI} dx + \int_0^2 \frac{(0.24x^2 - 1.2x)}{EI} dx$$

$$\Delta = -0.16 \left(\frac{x^3}{3} \right) \Big|_0^3 + 0.24 \left(\frac{x^3}{3} \right) \Big|_0^2 - 1.2 \left(\frac{x^2}{2} \right) \Big|_0^2$$

$$A = \frac{-0.16x^3}{3} + \frac{0.24x^3}{3} - \frac{1.2x^2}{2}$$

Silky

$$\begin{array}{r}
 -\frac{0.0533x^3}{1} + \frac{0.08x^3}{1} - \frac{0.6x^2}{1} \\
 -\frac{0.0533(3)^3}{IE} + \frac{0.08(2)^3}{IE} - \frac{0.6(2)^2}{IE} \\
 -\frac{0.0533(27)}{EI} + \frac{0.08(8)}{EI} - \frac{0.6(4)}{EI} \\
 -\frac{1.4391}{EI} + \frac{0.64}{EI} - \frac{2.4}{EI} \\
 \Delta = \frac{-3.1991}{EI} \uparrow +
 \end{array}$$



• Determinar la deflexion en el centro de la viga.

1. Aplicar carga "p"

$$\sum M_0 =$$

$$C_y (6m) + 3 \text{ TON.m} + P(3m) = 0$$

$$C_y = -3 \text{ TON.m} / 6m + P(3m/6m)$$

$$C_y = -0.5 \text{ TON} + 0.5 P$$

$$A_y - P - C_y = 0$$

$$A_y - P(0.5 \text{ TON} + 0.5 P)$$

$$A_y = 0.5 P + 0.5 \text{ TON}$$

CORTE 1

$$0 \leq x \leq 3$$

$$M_1 = 0.5 P(x) - 0.5 \text{ TON}(x)$$

$$0.5 P - 0.5 \text{ TON}$$

$$0 \leq x \leq 3$$

$$M_2 = 0.5 \text{ TON}(x) + 0.5 P(x)$$

$$-0.5 \text{ TON} + 0.5 P$$

$$a_m / a_p = 0.5 \times M_1$$

$$a_m / a_p = 0.5 \times M_2$$

formula

$$\Delta = \int_0^L \frac{m(x) \left(\frac{a_m}{a_p} \right)}{EI} dx$$

$$\Delta = \int_0^3 \frac{(-0.5x)(0.5x)}{EI} dx + \int_0^3 \frac{(0.5x+3)(0.5x)}{EI} dx$$

$$\Delta = \int_0^3 \frac{-0.25x^2}{EI} dx + \int_0^3 \frac{(0.25x^2 + 1.5x)}{EI} dx$$

$$\Delta = \frac{1}{EI} \left[-0.25 \left(\frac{x^{2+1}}{2+1} \right) \Big|_0^3 + \frac{1}{EI} \left[0.25 \left(\frac{x^{2+1}}{2+1} \right) \Big|_0^3 + 1.5 \left(\frac{x^{1+1}}{1+1} \right) \Big|_0^3 \right] \right.$$

$$\left. - \frac{0.25x^3}{3} - \frac{0.25x^3}{3} + \frac{1.5x^2}{2} \right]$$

$$= \frac{-0.08333(3)^3}{1} - \frac{0.08333(3)^3}{1} + \frac{0.75(3)^2}{1}$$

$$= \frac{-0.08333(27)}{IE} - \frac{0.08333(27)}{IE} + \frac{0.75(9)}{IE}$$

$$= \frac{-2.24991}{IE} + \frac{2.24991}{IE} + \frac{6.75}{IE}$$

$$\Delta = \frac{6.75}{IE}$$