

5 años de 2, 3, 5, 7 y 8
 años peso 14, 20, 32, 42 y 44

| Años | Kg | $(X+Y)$ | $(X+X)$ | $(Y+Y)$ |
|------|----|---------|---------|---------|
| X | Y | XY | X^2 | Y^2 |
| 2 | 14 | 28 | 4 | 196 |
| 3 | 20 | 60 | 9 | 400 |
| 5 | 32 | 160 | 25 | 1,024 |
| 7 | 42 | 294 | 49 | 1,764 |
| 8 | 44 | 352 | 64 | 1,936 |

Sumatorias

25 - 152 - 894 - 151 - 5,320

Sumas de cuadrados!

$$SCX = \sum X^2 - \frac{(\sum X)^2}{n} = 151 - \frac{(25)^2}{5} = \underline{SCX = 26}$$

$$SCY = \sum Y^2 - \frac{(\sum Y)^2}{n} = 5,320 - \frac{(152)^2}{5} = \underline{SCY = 700}$$

$$SCXY = \sum XY - \frac{(\sum X)(\sum Y)}{n} = 894 - \frac{(25)(152)}{5} = \underline{SCXY = 134}$$

Factor de Correlación!

$$r = \frac{SCXY}{\sqrt{SCX} \sqrt{SCY}} = \frac{134}{\sqrt{26} \sqrt{700}} = \underline{r = 0.99}$$

Fuerte +

Regresión Lineal.

$$1 = b_1 = \frac{SC_{XY}}{SC_X}$$

$$b_1 = \frac{134}{26} = 5.15 = b_1$$

$$2 = \bar{X} = \frac{\sum X}{n} = \frac{25}{5} = 5 = \bar{X}$$

$$\bar{Y} = \frac{\sum Y}{n} = \frac{152}{5} = 30.4 = \bar{Y}$$

$$3 = b_0 = \bar{Y} - b_1 * \bar{X}$$

$$b_0 = 30.4 - 5.15 * 5$$

$$30.4 - 25.75 = 4.65 = b_0$$

$$4 = \text{MRL } \hat{Y} = b_0 + b_1 * \hat{X}$$

(conocer KgS) $\hat{Y} = 4.65 + 5.15 * 7$

$$4.65 + 36.05 = 40.7 = \hat{Y}$$

← KgS

$$5 = \text{MRL } \hat{X} = \frac{\hat{Y} - b_0}{b_1} \quad \hat{X} = \frac{40.7 - 4.65}{5.15}$$

$$\hat{X} = \frac{36.05}{5.15}$$

$$\hat{X} = 6.99 \leftarrow \text{Años}$$

Las notas obtenidas por 5 alumnos
en matemáticas son:

| Mate | Q.M. | X^2 | X^2 | Y^2 |
|------|------|-------|--------|-------|
| X | Y | | | |
| 6 | 6.5 | 39 | 36 | 42.25 |
| 4 | 4.5 | 18 | 16 | 20.25 |
| 8 | 7 | 56 | 64 | 49 |
| 5 | 5 | 25 | 25 | 25 |
| 3.5 | 4 | 14 | 12.25 | 16 |
| 26.5 | 27 | 152 | 153.25 | 152.5 |

Suma de cuadrados:

$$De "X" = S_{cx} = \frac{\sum X^2}{n} - \frac{(\sum X)^2}{n^2} = 140.45$$

$$153.25 - 140.45 = 12.8$$

$$De "Y" = S_{cy} = \frac{\sum Y^2}{n} - \frac{(\sum Y)^2}{n^2} = 152.25 - \frac{(27)^2}{5}$$

$$152.25 - 145.8 = 6.45$$

$$Y = 6.7$$

$$De "XY" = \frac{\sum XY}{n} - \frac{(\sum X)(\sum Y)}{n^2}$$

$$152 - \frac{(26.5)(27)}{5} = 152 - 143.1$$

$$XY = 8.9$$

Factor de correlación

$$r = \frac{SC_{XY}}{\sqrt{SC_X} \sqrt{SC_Y}} = r = \frac{8.9}{\sqrt{(12.8)(6.7)}}$$

$$r = \frac{8.9}{\sqrt{85.76}} = r = \frac{8.9}{9.26}$$

$$r = 0.96 = \text{Fuerte}$$

Regresión Lineal

$$1: b_1 = \frac{SC_{XY}}{SC_X} = \frac{8.9}{12.8} = b_1 = 0.69$$

$$2: \bar{x} = 5.3 \quad \bar{y} = 5.4$$

$$3: b_0 = \bar{y} - b_1 * \bar{x} = 5.4 - (0.69)(5.3) \\ 5.4 - 3.65 = 1.75$$

$$4: \text{MRL } \hat{y} = b_0 + b_1 * \hat{x} = 1.75 + (0.69) \hat{x}$$

$$5: \text{MRL } \hat{x} = \frac{\hat{y} - b_0}{b_1} = \frac{\hat{y} - 1.75}{0.69}$$

Z : Un centro comercial se abre en función de la distancia, en Km, a la que se sitúa de un núcleo de población, según a los clientes, en cientos, que figuran en la tabla

Centros (distancia)

| X | Y | XY | X ² | Y ² |
|-----------|------------|------------|----------------|----------------|
| 8 | 15 | 120 | 64 | 225 |
| 7 | 19 | 133 | 49 | 361 |
| 6 | 25 | 150 | 36 | 625 |
| 4 | 23 | 92 | 16 | 529 |
| 2 | 34 | 68 | 4 | 1,156 |
| 1 | 40 | 40 | 1 | 1,600 |
| <u>28</u> | <u>156</u> | <u>603</u> | <u>170</u> | <u>4,496</u> |

Suma de cuadrados...

$$\textcircled{1} \text{ De } "x" = \frac{\sum X^2 - \frac{(\sum X)^2}{n}}{n} = \frac{170 - \frac{784}{6}}{6} = 130.66$$

$$170 - 130.66 = 39.34 = SCX$$

$$\textcircled{2} \text{ De } "y" = \frac{\sum Y^2 - \frac{(\sum Y)^2}{n}}{n} = \frac{4,496 - \frac{24,336}{6}}{6} = 4,056$$

$$4,496 - 4,056 = 440 = SCY$$

$$\textcircled{3} \text{ De } "xy" = \frac{\sum XY - \frac{(\sum X)(\sum Y)}{n}}{n} = \frac{603 - \frac{728}{6}}{6}$$

$$603 - 728 = -125 = SCXY$$

$$r = \frac{SC_{XY}}{\sqrt{(SC_X)(SC_Y)}} = \frac{-125}{\sqrt{(39.34)(440)}} = \frac{-125}{\sqrt{17,309.6}}$$

$$\frac{-125}{131.56} = -0.95 = \text{Factor de correlación}$$

Regresión Lineal

$$b_1 = \frac{SC_{XY}}{SC_X} = \frac{-125}{39.34} = \underline{-3.17 = B_1}$$

$$\textcircled{2} \bar{X} = 4.66, \bar{Y} = 26$$

$$\textcircled{3} b_0 = \bar{Y} - b_1 * \bar{X} = b_0 = 26 - (-3.17) * 4.66$$

$$26 - (-14.77) = \underline{40.77 = B_0}$$

$$\textcircled{4} MRL \hat{Y} = B_0 + B_1 * \hat{X} = 40.77 + (-3.17)(5)$$

$$40.77 + (-15.85) = \underline{24.92 \text{ KM}}$$

$$\textcircled{5} MRL \hat{X} = \frac{\hat{Y} - b_0}{b_1} = \frac{2 - 40.77}{(-3.17)} = \underline{\underline{\frac{(-38.77)}{(-3.17)}}}$$

$$= \underline{12.23 \text{ clientes por esperar}}$$

$$P(0.5) = (1.58, 1.8 - 2.25, 2.8$$

$$= (1.58)(1.02P(1) - 1.58)(1.8) - 2.25 = 1.58 * 1.02P(1) - 2.25$$

S: Las estaturas y Pesos de 10 jugadores de baloncesto de un equipo son:

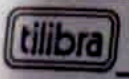
| Estatura | Peso | xy | x^2 | y^2 |
|--------------|------------|----------------|----------------|---------------|
| X | Y | | | |
| 186 | 85 | 15,810 | 34,596 | 7,225 |
| 189 | 85 | 16,065 | 35,721 | 7,225 |
| 190 | 86 | 16,340 | 36,100 | 7,396 |
| 192 | 90 | 17,280 | 36,864 | 8,100 |
| 193 | 87 | 16,791 | 37,249 | 7,569 |
| 193 | 91 | 17,563 | 37,249 | 8,281 |
| 198 | 93 | 18,414 | 39,204 | 8,649 |
| 201 | 103 | 20,703 | 40,401 | 10,609 |
| 203 | 100 | 20,300 | 41,209 | 10,000 |
| 205 | 101 | 20,705 | 42,025 | 10,201 |
| <u>1,950</u> | <u>921</u> | <u>179,971</u> | <u>380,618</u> | <u>85,255</u> |

(2) Suma de cuadrados...

① De " x " = $scx = \frac{\sum x^2 - (\sum x)^2}{n} = \frac{380,618 - \frac{(1,950)^2}{10}}{10} = \frac{380,618 - 380,250}{10} = \frac{368}{10} scx$

② De " y " = $scy = \frac{\sum y^2 - (\sum y)^2}{n} = \frac{85,255 - \frac{(921)^2}{10}}{10} = \frac{85,255 - 84,824.1}{10} = \frac{430.9}{10} scy$

③ De " xy " = $sctxy = \frac{\sum xy - (\sum x)(\sum y)}{n} = \frac{179,971 - (1,950)(921)}{10} = \frac{179,971 - 179,595}{10} = \frac{376}{10} scxy$



$$r = \frac{sc_{xy}}{\sqrt{sc_x} \sqrt{sc_y}} = \frac{376}{\sqrt{368} \sqrt{430.91}} = \frac{376}{\sqrt{158,571.2}}$$

$$\frac{376}{398.20} = \underline{0.94} = \text{Factor de correlación FUERTE}$$

Regresión Lineal

$$\textcircled{1} B_1 = \frac{sc_{xy}}{sc_x} = \frac{376}{368} = \underline{1.02 \text{ B1}}$$

$$\textcircled{2} \bar{x} = 195 \quad \bar{y} = 92.1$$

$$\textcircled{3} B_0 = \bar{y} - B_1 * \bar{x} = 92.1 - (1.02)(195) \\ 92.1 - 198.9 = \underline{-106.8 \text{ B0}}$$

$$\textcircled{4} \text{MRL } \hat{y} = B_0 + B_1 * \hat{x} = (-106.8) + (1.02)(208) \\ (-106.8) + 212.16 = \underline{105.36 \text{ Peso Kg}}$$

$$\textcircled{5} \text{MRL } \hat{x} = \frac{\hat{y} - B_0}{B_1} = \text{No pide el problema jeje...}$$

Si A partir de los siguientes datos referidos a hrs. trabajadas, Determina la recta de regresión de "Y" sobre "X".

| Horas | Producción | | | |
|------------|--------------|----------------|------------------|----------------|
| X | Y | X ² | Y ² | XY |
| 80 | 300 | 6,400 | 90,000 | 24,000 |
| 79 | 302 | 6,241 | 91,204 | 23,858 |
| 83 | 315 | 6,889 | 99,225 | 26,145 |
| 84 | 330 | 7,056 | 108,900 | 27,720 |
| 78 | 300 | 6,084 | 90,000 | 23,400 |
| 60 | 250 | 3,600 | 62,500 | 15,000 |
| 82 | 300 | 6,724 | 90,000 | 24,600 |
| 85 | 340 | 7,225 | 115,600 | 28,900 |
| 79 | 315 | 6,241 | 99,225 | 24,885 |
| 84 | 330 | 7,056 | 108,900 | 27,720 |
| 80 | 310 | 6,400 | 96,100 | 24,800 |
| 62 | 240 | 3,844 | 57,600 | 14,880 |
| 936 | 3,632 | 73,760 | 1,109,254 | 285,908 |

$$\textcircled{1} \text{De "X"} = \frac{SCX}{n} = \frac{\sum X^2 - \frac{(\sum X)^2}{n}}{n} = \frac{876,096 - \frac{73,008^2}{12}}{12}$$

$$= \frac{73,760 - 73,008}{12} = \boxed{752 \text{ SCX}}$$

$$\textcircled{2} \text{De "Y"} = \frac{SCY}{n} = \frac{\sum Y^2 - \frac{(\sum Y)^2}{n}}{n} = \frac{13,191,424 - \frac{1,109,254^2}{12}}{12}$$

$$= \frac{1,109,254 - 1,099,285,33}{12} = \boxed{9,968,67 \text{ SCY}}$$

$$\textcircled{3} \text{ De "xy" } = \frac{\sum xy - (\sum x)(\sum y)}{n} = \frac{(936)(3,632)}{12}$$

$$285,908 - 283,296 = \underline{2,612 \text{ SCXY}}$$

$$r = \frac{\text{SCXY}}{\sqrt{(\text{SCX})(\text{SCY})}}$$

$$r = \frac{2,612}{\sqrt{(752)(9,968.67)}} = \frac{2,612}{\sqrt{7,496,439.84}}$$

$$\frac{2,612}{2,737.96} = \underline{0.95} \text{ Factor de Correlación Fuerte.}$$

Regresión Lineal

$$\textcircled{1} B_1 = \frac{\text{SCXY}}{\text{SCX}} = \frac{2,612}{752} = \underline{3.47 \text{ B}_1}$$

$$\textcircled{2} \underline{\bar{x} = 78}, \underline{\bar{y} = 302.66}$$

$$\textcircled{3} B_0 = \bar{y} - b_1 * \bar{x} = 302.66 - (3.47)(78)$$

$$302.66 - 270.66 = \underline{32 \text{ B}_0}$$