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Grado: 6

Materia: Matemática aplicada

Nombre del trabajo: EJERCICIOS 4

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$$\int \sqrt{16x^2 - 1} dx \quad v^2 = 16x^2 \quad v = 4x \quad dv = 4 \quad a^2 = 1 \quad a = 1$$

$$\frac{1}{4} \frac{4x}{2} \sqrt{16x^2 - 1} = \frac{1}{2} \ln |4x + \sqrt{16x^2 - 1}| + c$$

$$\frac{4x}{8} \sqrt{16x^2 - 1} - \frac{1}{2} \ln |4x + \sqrt{16x^2 - 1}| + c$$

$$\int \sqrt{4 - 4x^2} dx \quad v^2 = 4x^2 \quad v = 2x \quad dv = 2 \quad a^2 = 4 \quad a = 2$$

$$\frac{1}{2} \frac{2x}{2} \sqrt{4 - 4x^2} + \frac{4}{2} \arcsin \frac{2x}{2}$$

$$\frac{2x}{4} \sqrt{4 - 4x^2} + \frac{4}{2} \arcsin \frac{2x}{2} + c$$

$$\int \frac{dx}{\sqrt{x^2 - 16}} \quad v^2 = x^2 \quad v = x \quad dv = 1 \quad a^2 = 16 \quad a = 4$$

$$2 \left(\frac{1}{4} \right) \ln \left| \frac{x+4}{x-4} \right| + c \quad \frac{1}{8} \ln \left| \frac{x+4}{x-4} \right| + c$$

$$\int \frac{dx}{16x^2 + 25} \quad v^2 = 16x^2 \quad v = 4x \quad dv = 4 \quad a^2 = 25 \quad a = 5$$

$$\frac{1}{4} \frac{1}{5} \arcsin \frac{4x}{5} + c \quad \frac{1}{20} \arcsin \frac{4x}{5} + c$$

$$\int \frac{dx}{2x} \sqrt{4x^2 - 1} \quad v^2 = 4x^2 \quad v = 2x \quad dv = 2 \quad a^2 = 1 \quad a = 1$$

$$\frac{1}{2} \arcsin \frac{2x}{1} + c$$

$$\int \frac{dx}{\sqrt{81x^2-9}} \quad v^2 = 81x^2 \quad v = 9x \quad dv = 9 \quad \frac{1}{9} \ln |4x + \sqrt{81x^2-9}| + C$$

$$\int \frac{dx}{4x^2-4} \quad v^2 = 4x^2 \quad v = 2x \quad dv = 2 \quad a^2 = 1 \quad a = 2 \quad \frac{1}{2} \frac{1}{4} \ln \left| \frac{2x-2}{2x+2} \right| + C = \frac{1}{8} \ln \left| \frac{2x-2}{2x+2} \right|$$

$$\int \frac{dx}{16-4x^2} \quad v^2 = 4x^2 \quad v = 2x \quad dv = 2 \quad a^2 = 16 \quad a = 4 \quad \frac{1}{2} \frac{1}{8} \ln \left| \frac{4+2x}{4-2x} \right| + C$$

$$\frac{1}{16} \ln \left| \frac{4+2x}{4-2x} \right| + C$$

$$\int \frac{dx}{\sqrt{4x^2+9}} \quad v^2 = 4x^2 \quad v = 2x \quad dv = 2 \quad a^2 = 9 \quad a = 3 \quad \frac{1}{2} \ln |2x + \sqrt{4x^2+9}| + C$$

$$\int \frac{dx}{3x\sqrt{9x^2-1}} \quad v^2 = 9x^2 \quad v = 3x \quad dv = 3 \quad a^2 = 1 \quad a = 1 \quad \frac{1}{3} \operatorname{arcsec} \frac{3x}{1} + C$$

$$\int \frac{\sqrt{25-4x^2}}{\operatorname{arc} \operatorname{Sen} \frac{2x}{5}} \quad v^2 = 4x^2 \quad v = 2x \quad dv = 2 \quad a^2 = 25 \quad a = 5 \quad \frac{1}{2} \frac{2x}{2} \sqrt{25-4x^2} + \frac{25}{2}$$

$$\int \frac{dx}{\sqrt{4x^2+1}} = v^2 = 4x^2 \quad v = 2x \quad dv = 2 \quad a^2 = 1 \quad a = 1 \quad \frac{1}{2} \ln |2x + \sqrt{4x^2+1}| + C$$

$$\int \frac{dx}{\sqrt{x^2+4}} \quad v^2 = x^2 \quad v = x \quad dv = 1 \quad a^2 = 4 \quad a = 2$$

$$\ln |Cx \sqrt{x^2+4}| + C$$

$$\int \frac{dx}{49-x^2} \quad v^2 = x^2 \quad v = x \quad dv = 1 \quad a^2 = 49 \quad a = 7$$

$$\frac{1}{2} (7) \ln \left| \frac{7+x}{7-x} \right| + \frac{1}{4} \ln |7+x| + C$$

$$\int \frac{dx}{\sqrt{4x^2+4}} \quad v^2 = 4x^2 \quad v = 2 \quad dv = 4 \quad a^2 = 1$$

$$\frac{1}{2} \ln |2x \sqrt{4x^2+4}|$$

$$\frac{1}{2} (4) \ln \left| \frac{4x^2-4}{4x^2+4} \right| + \frac{1}{11} \ln \left| \frac{4x^2-4}{4x^2+4} \right| + C$$