



**Universidad del sureste
Licenciatura en medicina
Humana.**



Tema: A derivar se ha dicho.

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Grupo: C

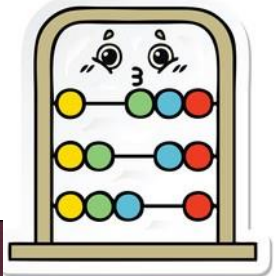
Grado: 2

Materia: Biomatemáticas .

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DERIVADAS



16/03/2022

"DERIVADAS"

Derivadas $f'(x)$

$f(x) = \frac{\Delta y}{\Delta x}$

$y = f(x)$

x_0

Derivada de la función en el punto marcado es equivalente a la pendiente de la recta de la tangente.

$t_b \rightarrow v \cdot \text{depend}$
 $t_a \rightarrow v \cdot \text{independiente}$
 $t_0 \rightarrow$

Reglas de la derivación:

- $f(x) = 0$
 $f'(x) = 0$
- $f(x) = 7$
 $f'(x) = 0$
- $f(x) = x^n$
 $f'(x) = nx^{n-1}$
- $f(x) = x^5$
 $f'(x) = 5x^4$
- $f(x) = cx$
 $f'(x) = (f(x))' = (c)'(x)$
- $f(x) = 3x^5$
 $f'(x) = 15x^4$

Ejercicios

DERIVADAS

- a) $x^1 = 3x^0$
- b) $x^2 = 2x^1$
- c) $x^3 = 3x^2$
- d) $x^4 = 4x^3$
- e) $x^5 = 5x^4$
- f) $x^6 = 6x^5$
- g) $x^7 = 7x^6$
- h) $x^8 = 8x^7$
- i) $x^9 = 9x^8$
- j) $x^{10} = 10x^9$
- k) $x^{11} = 11x^{10}$
- l) $x^{12} = 12x^{11}$
- m) $x^{13} = 13x^{12}$
- n) $x^{14} = 14x^{13}$
- o) $x^{15} = 15x^{14}$
- p) $x^{16} = 16x^{15}$
- q) $x^{17} = 17x^{16}$
- r) $x^{18} = 18x^{17}$
- s) $x^{19} = 19x^{18}$
- t) $x^{20} = 20x^{19}$

- 1) $4x^3 = 12x^2$
- 2) $5x^6 = 30x^5$
- 3) $7x = 7$
- 4) $3x^3 = 9x^2$
- 5) $8x^2 = 16x$

Reglas de la derivación

$$4.- f(x) = f \pm g$$

$$f'(x) = (f \pm g)' = f' \pm g'$$

$$f(x) = 2x^3 + x$$

$$f'(x) = 2(3x^2) + 1$$

$$= 6x^2 + 1$$

- 1) $2x^2 + 3x = 4x + 3x$
- 2) $6x - 2 = 6$
- 3) $5x^5 + x^2 = 25x^4 + 2x$
- 4) $7x^2 + x = 14x + 1$
- 5) $9x^3 - 4x = 27x^2 - 4$

Reglas de la derivación

$$1) 2x^2 + 3x$$

$$2(2x) + 3x$$

$$= 4x + 3x$$

$$2) 6x - 2$$

$$6(x) - 2$$

$$= 6 - 2$$

$$3) 5x^5 + x^2$$

$$5(5x^4) + 2x$$

$$25x^4 + 2x$$

$$4) 7x^2 + x$$

$$2(7x) + x$$

$$14x + x$$

$$5) 9x^3 - 4x$$

$$9(3x^2) - 4x$$

$$27x^2 - 4x$$

Reglas de la derivación:

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$$5. f(x) = fg + fg$$

$$f'(x) = (fg)' = fg' + fg'$$

$$f(x) = (4x+1) + (10x^2-5)$$

$$f'(x) = 20x(4x+1) + 4(10x^2-5)$$

Ejercicios:

$$1) (4x^3-2) - (6x^2+2)$$

$$f'(x) = 8x(4x^3-2) - 4(6x^2+2)$$

$$2) (3x^5+5x) + (7x-3)$$

$$f'(x) = 7x(3x^5+5x) + 3(7x-3)$$
$$15x^4 + 5(7x-3)$$

$$3) (5x^2-6) + (8x^3+4)$$

$$f'(x) = 20x(5x^2-6) + 5(8x^3+4)$$

Corrección:

$$f'(x)$$

$$4) (2x^2 - 3x) - (6x - 1)$$

$$f'(x) = 2x(2x^2 - 3x) - 2(6x - 1)$$

$$5) (7x^3 + 7) + (7x^2 - 7)$$

$$f'(x) = 49x(7x^3 + 7) + 7(7x^2 - 7)$$

$$b) f(x) = \left[\frac{p}{q} \right] \quad f'(x) = \frac{p'q - pq'}{q^2}$$

$$f(x) = \frac{4x-5}{5x^2+3x}$$

$$\frac{[10x+3(4x-5)] - [4(5x^2+3x)]}{(5x^2+3x)^2}$$

EJERCICIOS:

$$1) \frac{6x^3+4}{2x^2+3x}$$

$$\frac{[8x+3(6x^3+4)]}{2x^2+3x} + \frac{[6(2x^2+3x)]}{(2x^2+3x)^2}$$

$$\frac{[4x+3(6x^3+4)]}{2x^2+3x} - \frac{[18x^2(2x^2+3x)]}{(2x^2+3x)^2}$$

$$2) \frac{5x^5-2x^4}{3x^3-x^2}$$

$$\frac{[5-x^2(5x^2-2x^4)]}{3x^3-x^2} - \frac{[5(3x^2-x^2)]}{(3x^3-x^2)^2}$$

$$\frac{[10x^2-2x(5x^3-2x^4)]}{(3x^3-x^2)^2} - \frac{[2x^4(3x^3-x^2)]}{(3x^3-x^2)^2}$$

$$3) \frac{4x^4+3x^3}{2x^2+x}$$

$$\frac{[4x+1(4x^4+3x^3)]}{(2x^2+x)^2} - \frac{[6x^3+0x^2(2x^2+x)]}{(2x^2+x)^3}$$

$$4) \frac{8x^2 - 3x}{2x}$$

$$f(x) = \frac{2(8x^2 - 3x)}{2x} = \frac{16x^2 - 6x}{2x}$$

$$5) \frac{x^2}{2x^3}$$

$$\frac{6x^2(x^2)}{2x^3(2x^3)} = \frac{6x^4}{4x^6}$$

Ejercicios:

$$1) f(x) = 3x^2$$

$$f(x) = 3x^2$$

$$f'(x) = 2(3x^{2-1})$$

$$f'(x) = 6x$$

Formula

$$f(x) = x$$

$$f'(x) = 1 \cdot x = 1 \cdot f'(x)$$

$$2) f(x) = 5$$

$$f(x) = 5$$

$$f'(x) = 0$$

$$f(x) = 0$$

$$f(x) = 0$$

$$3) f(x) = -2x$$

$$f(x) = 2x = -2(1)$$

$$f'(x) = -2$$

$$f(x) = x$$

$$f'(x) = 1 \cdot f'(x) = 1 \cdot f'(x)$$

$$4) f(x) = 2x^2 - 5$$

$$f(x) = 2x^2 - 5$$

$$f'(x) = 2(2x^{2-1}) - 0$$

$$f'(x) = 4x$$

$$f(x) = f + g$$

$$f'(x) = (f' + g')$$

$$f(x) = f' + g$$

$$5) f(x) = 2x^4 + x^3 - x^2 - 4$$

$$f(x) = 2x^4 + x^3 - x^2 - 4$$

$$f'(x) = 4(2x^{4-1}) + 3(x^{3-1}) - 2(x^{2-1})$$

$$= 8x^3 + 3x^2 - 2x$$

$$f(x) = f + g$$

$$f'(x) = (f' + g)'$$

$$f' + g$$

$$6) f(x) = 4x^3 + 6x$$

$$f(x) = 4x^3 + 6x$$

$$f'(x) = 3(4x^{3-1}) + 6(1)$$

$$f'(x) = 12x^2 + 6$$

$$f(x) = f + g = f'(x) = (f' + g)$$

$$f'(x) = f' + g$$

Formulas

7) $f(x) = 8x^6$

$f(x) = 8x^6$

$f'(x) = 6(8x^{6-1}) = 48x^5$

$f(x) = (x)$

$f'(x) = (f(x))' = (f^{-1}(x))'$

8) $f(x) = 8$

$f(x) = 8$

$f'(x) = 0$

$f(x) = 0$

$f'(x) = 0$

9) $(3x^3 + 2x) + (6x^4 + 6)$

$(3x^3 + 2x) + (6x^4 + 6) =$

$24x^3 + 3(3x^3 + 2x) + 9x^2 + 2(6x^4 + 6)$

$f(x) = fg \pm fg$

$f'(x) = (fg)' = fg' \pm fg$

10) $\frac{8x^6 - 6x^3 - 4}{2x^4}$

$\frac{8x^6 - 6x^3 - 4}{2x^4}$

$f(x) = \left[\frac{f}{g} \right]$

$f'(x) = \frac{f'g - fg'}{g^2}$

$= \frac{[8x^3(8x^6 - 6x^3 - 4) - (48x^3 - 18x^2)(2x^4)]}{2x^8}$

11) $(7x^2 + 4x) + (6x^3 - 2x^2)$

$(7x^2 + 4x) + (6x^3 - 2x^2)$

$(8x^2 - 4)(7x^2 + 4x) + 14x + 4(5x^3 - 2x^2)$

$f(x) = fg \pm fg$

$f'(x) = fg' \pm (fg)'$

Formula

12) $(3x^3 + 6) - (8x^2 - 2x)$

$f(x) = fg \pm fg$
 $f'(x) = (fg)' = fg' \pm$

$(3x^3 + 6) - (8x^2 - 2x)$
 $= 16x - 2(3x^3 + 6) - 12x^4 + 6(8x^2 - 2x)$

13) $\frac{2x^3 - x^2}{6x^2 + x + 2}$
 $\frac{2x^3 - x^2}{6x^2 + x + 2}$

$f(x) = fg \pm fg$
 $f'(x) = (fg)' = fg' \pm fg$

$\frac{d}{dx} \left[\frac{2x^3 - x^2}{6x^2 + x + 2} \right] = \frac{(6x^2 - 2x)(6x^2 + x + 2)}{6x^2 + x + 2}$

14) $(6x^4 + 2x^3) - (2x^6 + x^5)$

$(6x^4 + 2x^3) - (2x^6 + x^5)$
 $(2x^5 + 5x^4)(6x^4 + 2x^3) = 24x^9 + 10x^4(2x^6 + x^5)$

$f(x) = fg \pm fg$
 $f'(x) = (fg)' = fg' \pm fg$

15) $f(x) = 78$

$f(x) = 78$
 $f'(x) = 0$

$f(x) = 0$
 $f'(x) = 0$