



**Nombre del trabajo:  
Poniendo limites**

**Materia: Biomatemáticas**

**Nombre del alumno:  
Carlos Omar Jacob Velázquez**

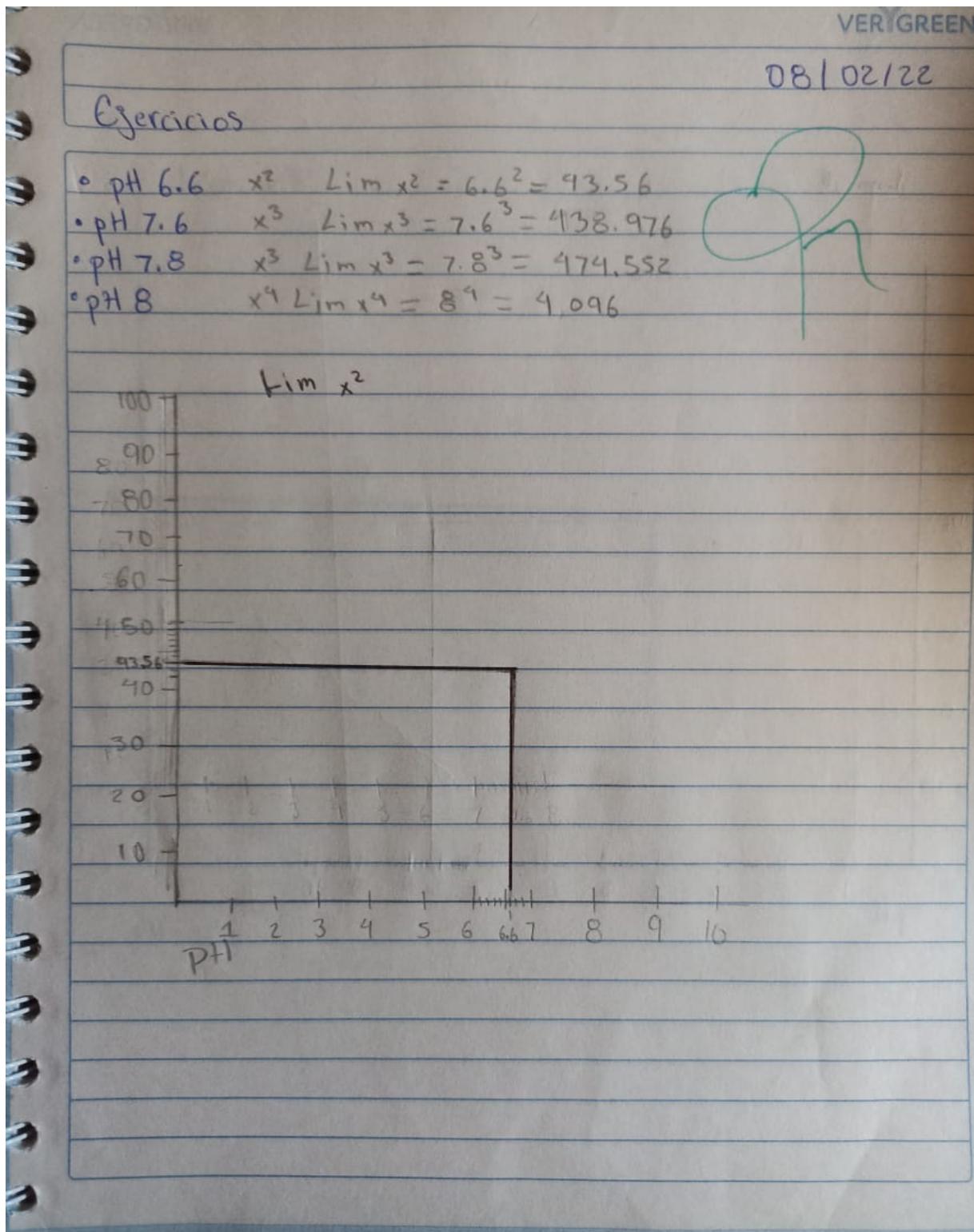
**Grado: 2**

**Grupo: A**

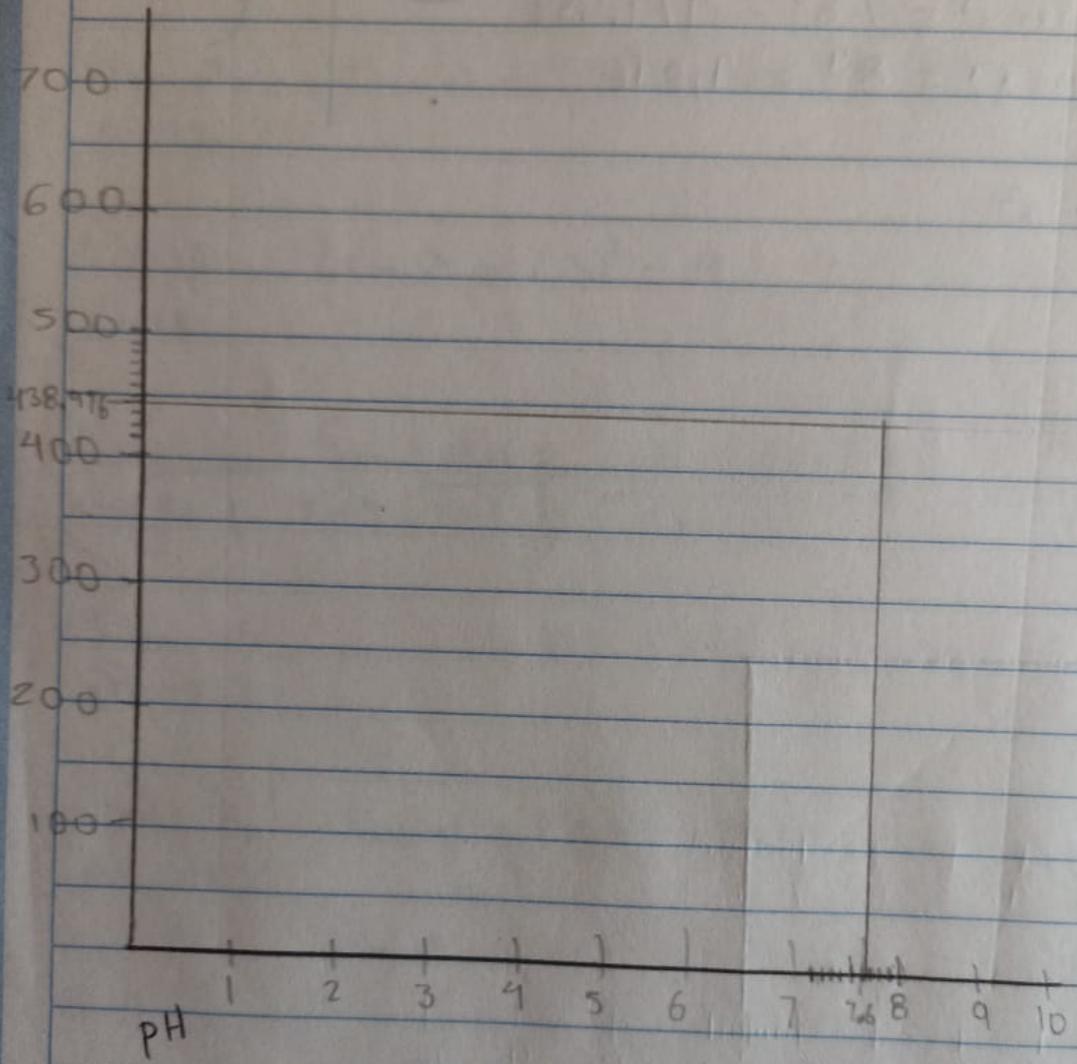
**Docente:**

**Dra. Rosvanni Margine Morales Irecta**

Realizar ejercicios puestos por el catedrático durante la clase, los cuales deben de estar calculados y graficados, tanto en el eje de "x" y eje de "y", tomando en cuenta los datos correspondientes a cada situación propuesta.



Lim x<sup>3</sup>



Lim x<sup>3</sup>

800

700

600

500

474.552

400

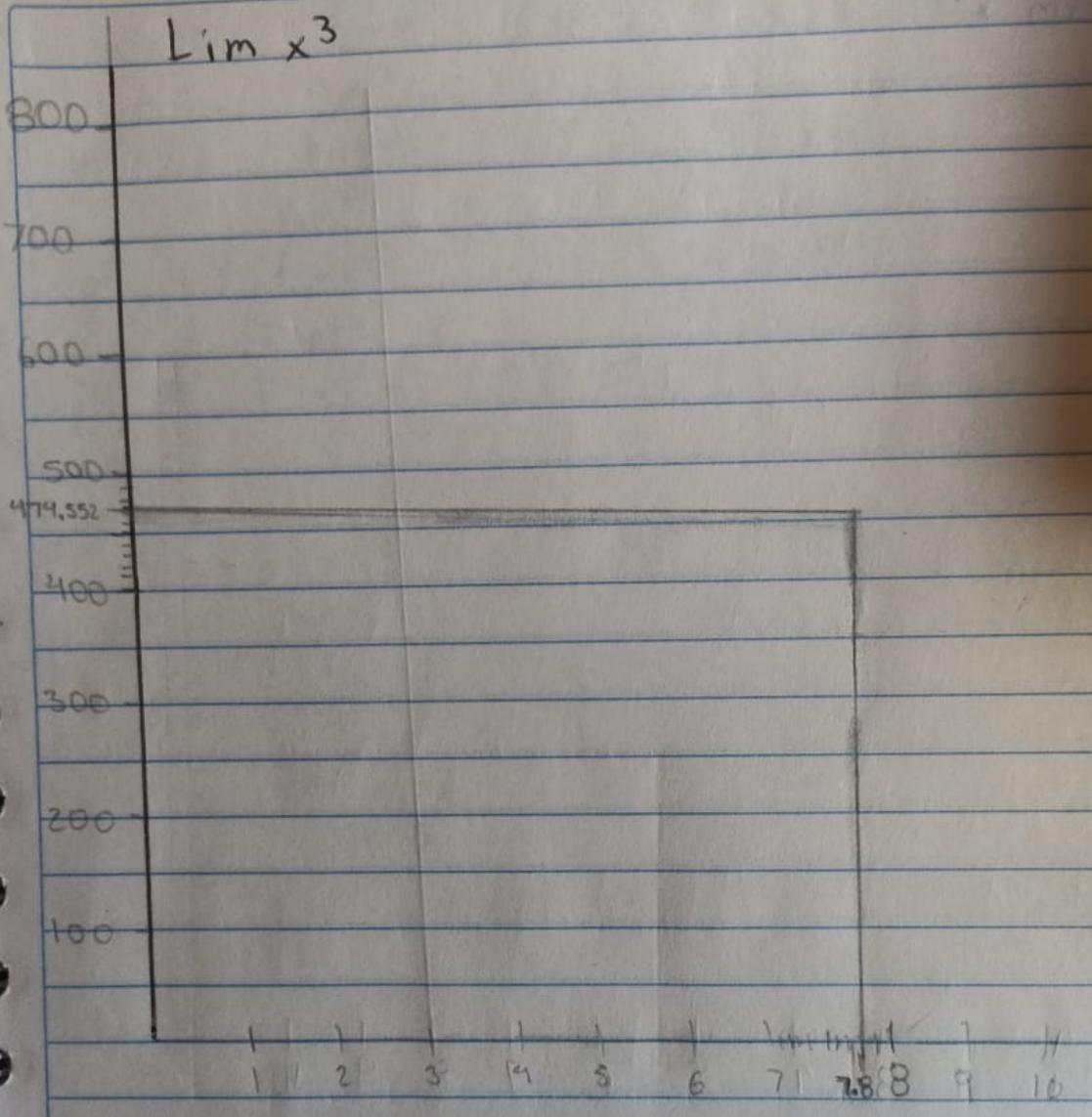
300

200

100

1 2 3 4 5 6 7 7.8 8 9 10

pH



4500  $\lim x^4$

4096  
4000

3500

3000

2500

2000

1500

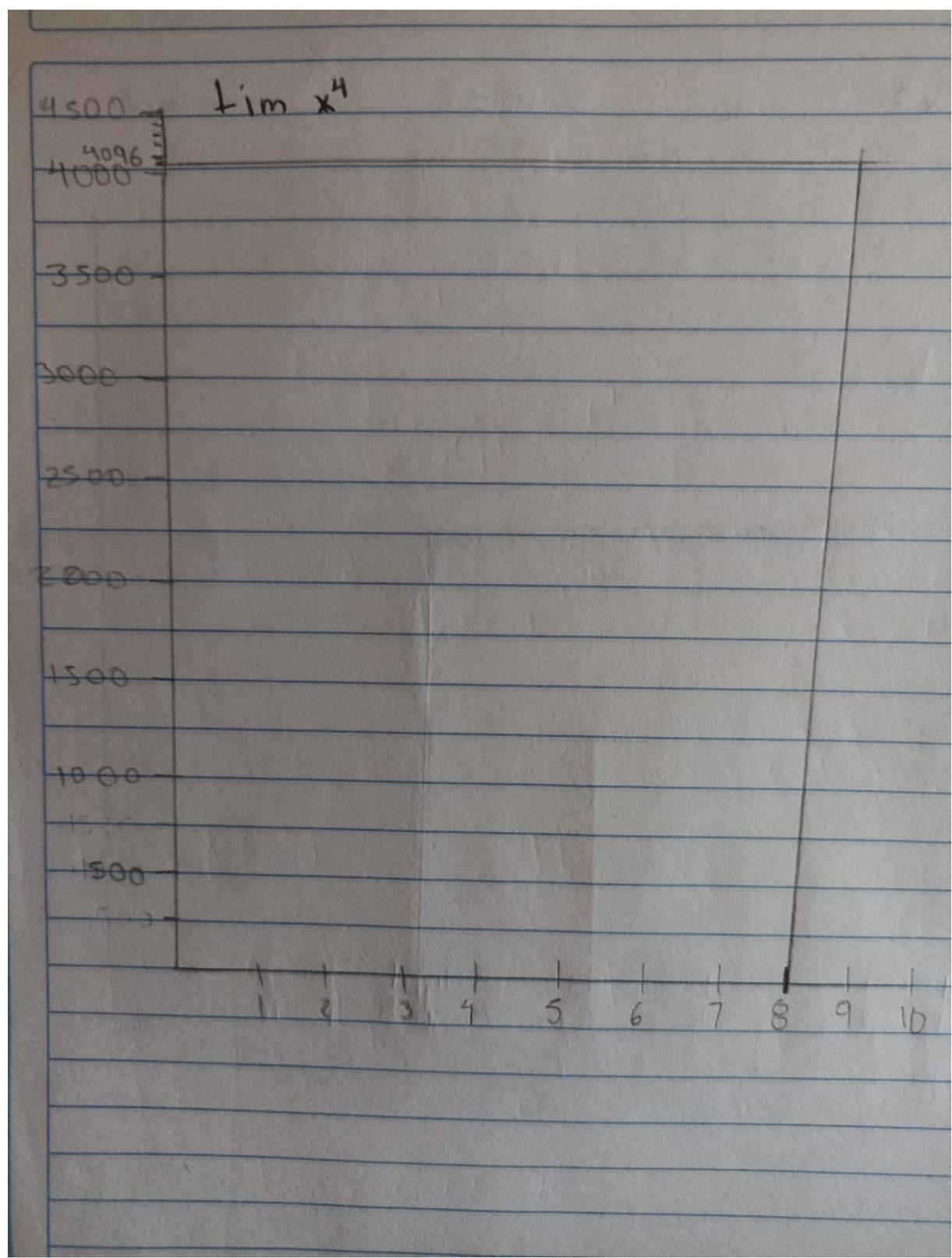
1000

500

1500

500

1 2 3 4 5 6 7 8 9 10



09/02/22

Ejercicios  $\lim x^2$

pH 6.6  $f(x)^2 = (6.6)^2 = 43.56$

pH 7.6  $f(x)^2 = (7.6)^2 = 57.76$

pH 7.8  $f(x)^2 = (7.8)^2 = 60.84$

pH 8  $f(x)^2 = (8)^2 = 64$

|      |   |    |
|------|---|----|
| 9096 | 2 |    |
| 2093 | 2 | >6 |
| 1043 | 3 |    |
| 1031 | 3 |    |
| 1011 |   |    |

15/02/22

Limites.

La constante 'd' no cambia.

1)  $\lim_{x \rightarrow a} c = c$        $\lim_{x \rightarrow 5} 5 = 5$

2)  $\lim_{x \rightarrow a} x = a$        $\lim_{x \rightarrow 4} x = 4$

3)  $\lim_{x \rightarrow a} x^n = a^n$        $\lim_{x \rightarrow 4} x^2 = 4^2$

4)  $\lim_{x \rightarrow a} \sqrt[n]{x} = \sqrt[n]{a}$        $\lim_{x \rightarrow 4} \sqrt[3]{4} = 2$        $\lim_{x \rightarrow 4} 2 = 2$

### Propiedades de los límites

1)  $\lim_{x \rightarrow 2} k[f(x)] = k \lim_{x \rightarrow 2} f(x) = kL$        $L = \text{límite}$

$\lim_{x \rightarrow 2} 4[f(x)] = 4 \lim_{x \rightarrow 2} f(x) = 4 \cdot 2 = 8$

0  $k \left[ \lim_{x \rightarrow 2} f(x) \right] = 4(2) = 8$

2)  $\lim_{x \rightarrow a} f(x) \pm g(x) = \lim_{x \rightarrow a} f(x) \pm \lim_{x \rightarrow a} g(x) = L \pm M$

$\lim_{x \rightarrow 3} 2x + 3x = 6 + 9 = 15$

0  $\lim_{x \rightarrow 3} (2(3)) + (3(3)) = 6 + 9$   
 $\lim_{x \rightarrow 3} = 15$

leer pag. 59.

$$3) \lim_{x \rightarrow a} f(x) * g(x) = \lim_{x \rightarrow a} f(x) * \lim_{x \rightarrow a} g(x) = L * M.$$

$$\lim_{x \rightarrow 7} [2x * 4x] = 6 * 12 = \underline{72}, \quad \lim = \underline{72}$$

$$4) \lim_{x \rightarrow a} f(x) \div g(x) = \lim_{x \rightarrow a} f(x) \div \lim_{x \rightarrow a} g(x) = L \div M, \quad M \neq 0$$

$$\lim_{x \rightarrow 2} \frac{f(x)}{g(x)} \quad \lim_{x \rightarrow 2} \frac{4x}{8x} = \frac{4(2)}{8(2)} = \frac{8}{16} = 0.5$$

$$\lim_{x \rightarrow 2} \frac{4x + 2x}{3x - 2x} = \frac{8 + 4}{6 - 4} = \frac{12}{2} = \underline{6}$$

$$5) \lim_{x \rightarrow a} x^n = a^n = \lim_{x \rightarrow a} f(x) = \lim_{x \rightarrow a} x^n$$

$$\lim_{x \rightarrow a} \sqrt[n]{f(x)} = \lim_{x \rightarrow a} \sqrt[n]{x}$$

$$= \sqrt[n]{a}$$

$$6) \text{ si } k \text{ es una constante } \lim_{x \rightarrow a} k = k$$

pH 6  
 pH 9  
 pH 5.5

1) pH 6

$$f(x) \quad k[f(x)] = 6(6) = \underline{36}$$

$x \rightarrow 6$

2) pH 9

$$f(x) \quad k[f(x)] = 9$$

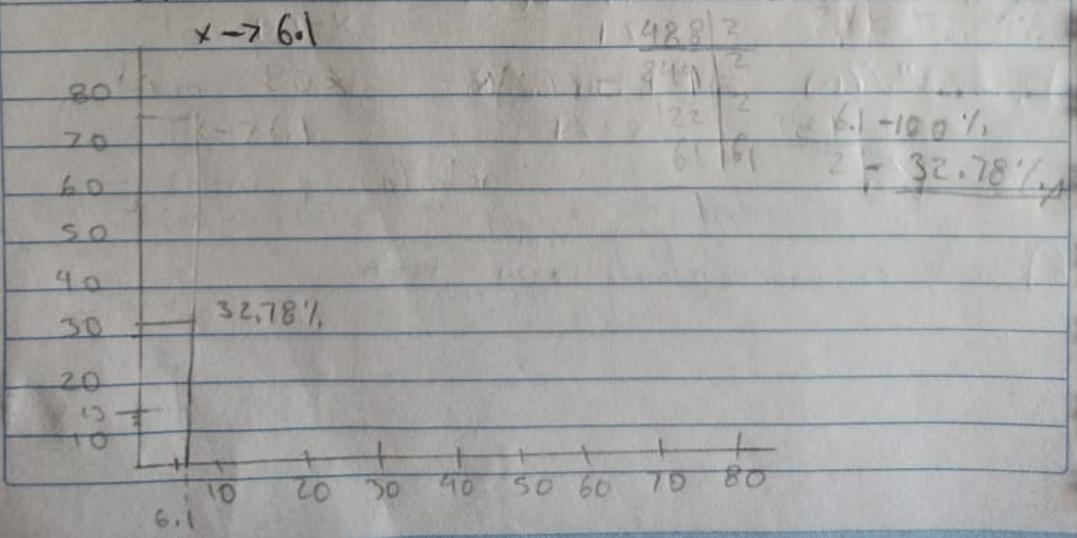
$$x \rightarrow 9 \quad 9[9] = \underline{81}$$

3) pH 5.5

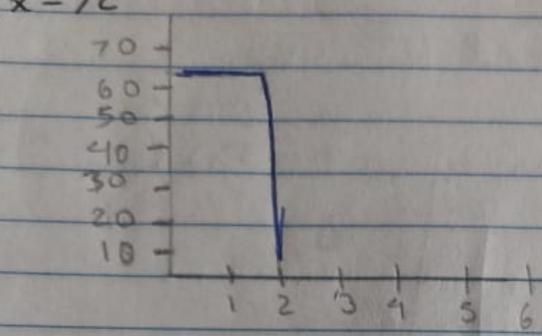
$$f(x) \quad k[f(x)] = 5.5(5.5) = \underline{30.25}$$

$x \rightarrow 5.5$

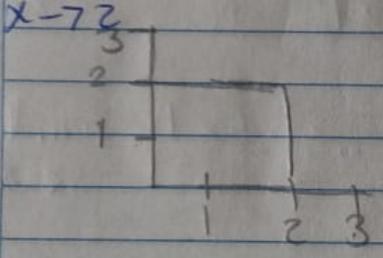
$$\lim_{x \rightarrow 6.1} 80 \times 80(6.1) = 488$$



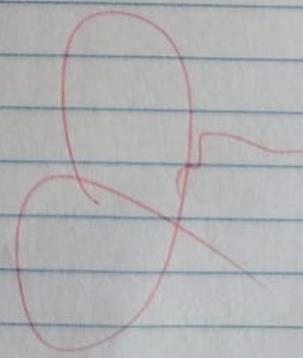
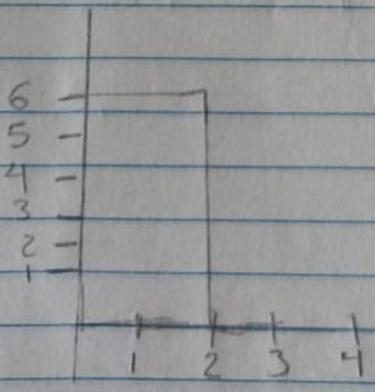
$$\lim_{x \rightarrow 2} [2x]^3 = [2(2)]^3 = 4^3 = \underline{64}$$



$$\lim_{x \rightarrow 2} \sqrt{2x} = \sqrt{2(2)} = \sqrt{4} = \underline{2}$$



$$\lim_{x \rightarrow 2} \frac{4x + 2x}{3x - 2x} = \frac{8 + 4}{6 - 4} = \frac{12}{2} = 6$$



16/02/22

## Límites laterales

• Cuando  $x$  se acerca a  $c$  por la derecha

$$\lim_{x \rightarrow a^+} f(x) \quad \delta \quad \lim_{x \rightarrow 0^+} \frac{|x|}{x}$$

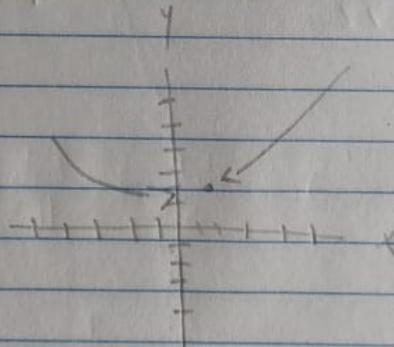
Cuando  $x$  se acerca a  $c$  por la izquierda

$$\lim_{x \rightarrow a^-} f(x) \quad \delta \quad \lim_{x \rightarrow 0^-} \frac{|x|}{x}$$

$$f(x) = \frac{|x|}{x} = \begin{cases} x^2 + 1 & \text{si } x < 1 \\ 2 & \text{si } x > 1 \end{cases}$$

$$\lim_{x \rightarrow 1} x^2 + 1 \quad |1+1=2$$

$$\lim_{x \rightarrow 1^+} 2 = 2$$



$$f(x) = \frac{|x|}{x} \begin{cases} x^2 & \text{si } x < 2 = 4 \\ 4 & \text{si } x = 2 \\ 6 - 2x & \text{si } x > 2 \end{cases}$$

$$\lim_{x \rightarrow 2^-} x^2 = 2^2 = 4$$

$$\lim_{x \rightarrow 2} 4 = 4$$

$$x \rightarrow 2$$

$$\lim_{x \rightarrow 2^+} 6 - 2(2) = 12$$

$$x \rightarrow 2^+ \quad x - 2$$

$$\lim_{x \rightarrow 2} 6 - 2x$$

$$x \rightarrow 2$$

