



**Nombre del trabajo:  
A seguir derivando**

**Materia: Biomatemáticas**

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**Grado: 2**

**Grupo: A**

**Docente:**

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# Reglas de la derivación.

1.-  $f(x) = c$        $f(x) = 7$   
 $f'(x) = 0$        $f'(x) = 0$

2.-  $f(x) = x^n$        $f(x) = x^3$   
 $f'(x) = nx^{n-1}$        $f'(x) = 3x^2$

3.-  $f(x) = cx$        $f(x) = 3x^5$        $f'(x) = 3(5x^4)$   
 $f'(x) = cf(x) = cf'(x)$        $15x^4$

4.-  $f(x) = f \pm g$        $f(x) = 2x^3 \pm x$   
 $f' = (f \pm g)' = f' \pm g'$        $f(x) = 6x^2 \pm 1$

## Ejercicios

$f(x) =$

- |                        |                     |
|------------------------|---------------------|
| 1) $x^5 = 5x^4$        | 1) $2x^6 = 12x^5$   |
| 2) $x^8 = 8x^7$ ✓      | 2) $9x^2 = 8x$      |
| 3) $x^9 = 9x^8$ ✓      | 3) $5x^3 = 15x^2$ ✓ |
| 4) $x^{11} = 11x^{10}$ | 4) $6x^4 = 24x^3$   |
| 5) $x^4 = 4x^3$        | 5) $10x^2 = 20x$    |

1)  $4x^3 + 2x = 12x^2 + 2$

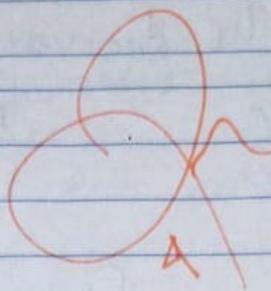
2)  $6x^2 - 3 = 12x$

3)  $2x^4 - x^2 = 8x^3 - 2x$

4)  $3x^6 + x = 18x^5 + 1$  ✓

5)  $x^7 - 3x = 7x^6 - 3$

Regla



5.)  $f(x) = fg + fg$   
 $f'(x) = fg' + f'g$

$f(x) = (4x+1) + (10x^2 - 5)$   
 $f'(x) = 20x(4x+1) + 4(10x^2 - 5)$

Ejercicios

1)  $(5x^2+2) + (3x-2) = 3(5x^2+2) + 10x(3x-2)$

2)  $(7x^3+2x) + (2x^2+5x) = 4x(7x^3+2x) + 21x^2(2x^2+5x)$

3)  $(2x+10) - (2x^3-10) = 6x^2(2x+10) - 2(2x^3-10)$

4)  $(8x^4+10x) + (6x-3) = 6(8x^4+10) + 32x^3(6x-3)$

5)  $(20x+2) - (8x^5+6) = 10x^4(20x+2) - 20x(8x^5+6)$

Regla 6

6.  $f(x) =$

1)  $4x^3 + 6x = 12x^2 + 6$

Regla 4

2)  $8x^6 = 48x^5 = 8(6x^5)$  ✓

Regla 3

3)  $7 = f'(x) = 0$

Regla 1

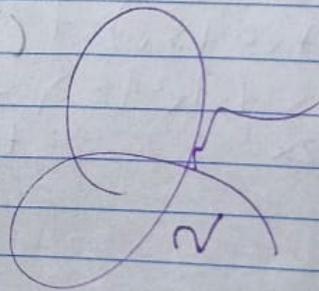
4)  $(3x^3 + 2x) + (6x^4 + 6) =$

$24x^3(3x^3 + 2x) + 9x^4(6x^4 + 6)$

Regla 5

5)  $(8x + 2) - (3x^2 - x) =$

$6x - 1(8x + 2) - 8x(3x^2 - x)$



6)  $(7x^2 + 4x) + (6x^3 - 2x^2) \cdot$

$18x^2(7x^2 + 4x) + 14x + 4(6x^3 - 2x^2)$

$18x^2 - 4x$

7)  $(2x^3 - 9x^2) + (2x + x) \cdot$

$2 + 1(2x^3 - 9x^2) + 6x^2(2x + x)$

$6x^2 - 8x$

8)  $(6x^4 + 2x^5) - (2x^6 + x^5) \cdot$

$12x^5(6x^4 + 2x^5) - 24x^3(2x^6 + x^5)$

$12x^3 + 5x^4$

$-24x^3 + 10x^4$

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Regla.

$$6. \quad (x) = \left(\frac{f}{g}\right)' = \frac{f'g - fg'}{g^2}$$

$$9) \quad (3x^5 + 6) - (8x^2 - 2x)$$

$$16x - 2(3x^5 + 6) - 15x^4(8x^2 - 2x)$$

$$10) \quad (9x^2 + 3x) + (x^3 + x^2)$$

$$3x^2(9x^2 + 3x) + 18x(x^3 + x^2)$$

$$3x^2 + 2x$$

$$+ 18x + 3$$

6)  $f(x) = \left(\frac{f}{g}\right)'$   $f'(x) = \frac{f'y - fy'}{g^2}$

ej.  $f(x) = \frac{4x+1}{10x^2-5} = \frac{20x(4x+1) - 4(10x^2-5)}{(10x^2-5)^2}$

Ejercicios.

1)  $f(x) = \frac{5x^2+4x}{6x^3} = \frac{18x(5x^2+4x) - (10x+4)(6x^3)}{(6x^3)^2}$  ✓

2)  $f(x) = \frac{3x^5-7x^4}{2x} = \frac{2(3x^5-7x^4) - (15x^4-28x^3)(2x)}{(2x)^2}$  ✓

3)  $f(x) = \frac{10x^2+5x}{15x-2} = \frac{15(10x^2+5x) - (20x+5)(15x-2)}{(15x-2)^2}$  ✓

4)  $f(x) = \frac{2x^{10}}{2x^5} = \frac{10x^4(2x^{10}) - 20x^9(2x^5)}{(2x^5)^2}$  ✓

5)  $f(x) = \frac{58x}{60x} = \frac{60(58x) - 58(60x)}{(60x)^2}$  ✓

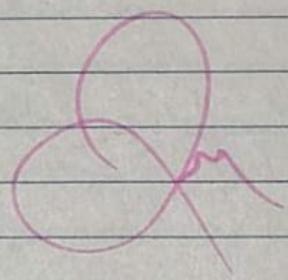
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Teorema: la derivada de 1 potencia entera de 1 función sea:  $y = [f(x)]^n$  entonces  $y' = n[f(x)]^{n-1} f'(x)$

Ej.  $f(x) = (2x+3)^3$   
 $f'(x) = (3) (2x+3)^{3-1} (2)$   
 $f'(x) = (3) (2x+3)^2 (2)$   
 $f'(x) = 6 (2x+3)^2$

Ejercicios

1)  $f(x) = (3x^4 - 5)^2$  ✓  
 $f'(x) = (2) (3x^4 - 5)^{2-1} (12x^3)$   
 $f'(x) = (2) (3x^4 - 5) (12x^3)$   
 $f'(x) = 24x^3 (3x^4 - 5)$



2)  $f(x) = (x+2)^3$  ✓  
 $f'(x) = (3) (x+2)^{3-1} (1)$   
 $f'(x) = (3) (x+2)^2 (1)$   
 $f'(x) = (3) (x+2)^2$

3)  $f(x) = (6x^2 - 5x + 4)^4$  ✓  
 $f'(x) = (4) (6x^2 - 5x + 4)^{4-1} (12x - 5)$   
 $f'(x) = (4) (6x^2 - 5x + 4)^3 (12x - 5)$   
 $f'(x) = 48x - 20 (6x^2 - 5x + 4)^3$

4)  $f(x) = (2xy - 3)^5$  ✓  
 $f'(x) = (5) (2xy - 3)^{5-1} (2y)$   
 $f'(x) = (5) (2xy - 3)^4 (2y)$   
 $f'(x) = 10 (2xy - 3)^4 y$

5)  $f(x) = (5x^2 + 4y - 3)^2 = (2) (5x^2 + 4y - 3)^{2-1} (10x + 4)$   
 $f'(x) = (2) (5x^2 + 4y - 3) (10x + 4)$   
 $f'(x) = 20x + 8 (5x^2 + 4y - 3)$

Tarea

22/03/22

1)  $f(x) = 3x^2 \rightarrow 6x$  ✓

2)  $f(x) = 5 \rightarrow 0$  ✓

3)  $f(x) = -2x \rightarrow -2$  ✓

4)  $f(x) = -2x + 2 \rightarrow -2$  ✓

5)  $f(x) = -2x^2 + 2 \rightarrow 4x$  ✓

6)  $f(x) = 9x^3 + 6x \rightarrow 12x^2 + 6$  ✓

7)  $f(x) = 8x^6 \rightarrow 48x^5$  ✓

8)  $f(x) = 7 \rightarrow 0$  ✓

9)  $f(x) = (3x^3 + 2x) + (6x^4 + 6) \rightarrow 24x^3(3x^3 + 2) + 9x^2 + 2(6x^4 + 6)$  ✓

10)  $f(x) = (8x + 2) - (3x^2 - x) \rightarrow 6x - 1(8x + 2) - (8)(3x^2 - x)$  ✓

11)  $f(x) = (7x^4 + 6x^3 - 5x^2 + x)^3$  ✓

12)  $f(x) = \frac{8x^6 - 6x^3 - 4}{2x^4}$  ✓

13)  $2x^3 - x^2 / 6x^2 + x + 2$  ✓

14)  $f(x) = 78 \rightarrow 0$  ✓

15)  $f(x) = (2x^3 + 5x^2 + 6x)^4$  ✓

11)  $f(x) = (7x^4 + 6x^3 - 5x^2 + x)^3$

$f(x) = (3)(7x^4 + 6x^3 - 5x^2 + x)^{3-1} \cdot (28x^3 + 18x^2 - 10x + 1)$

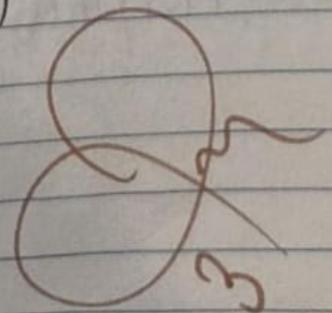
12)  $f(x) = 8x^6 - 6x^3 - 4 / 2x^4 = 8x^3(8x^6 - 6x^3 - 4) - 48x^5 - 18x^2(2x^4) / (2x^4)^2$

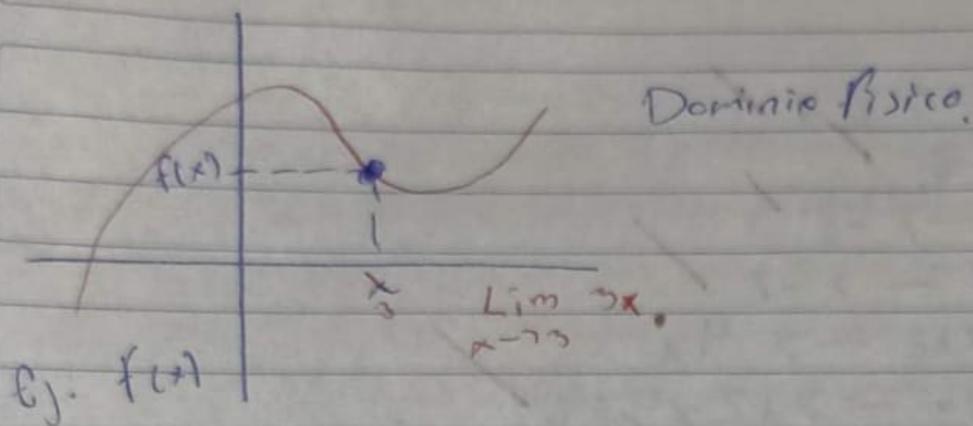
13)  $f(x) = 2x^3 - x^2 / 6x^2 + x + 2 = 12x + 1(2x^3 - x^2) - 6x^2 - 3x^2(6x^2 + x + 2) / (6x^2 + x + 2)^2$

15)  $f(x) = (2x^3 + 5x^2 + 6x)^4$

$f(x) = (4)(2x^3 + 5x^2 + 6x)^{4-1} \cdot (6x^2 + 10x + 6)$

$f(x) = 24x^2 + 40x + 24(2x^3 + 5x^2 + 6x)^3$





Ejercicios

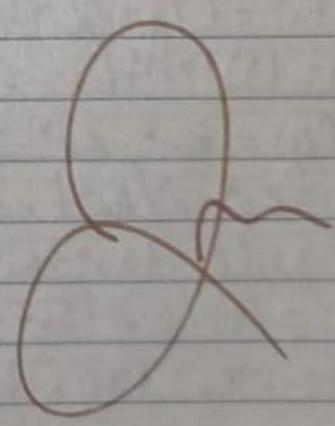
1)  $(x=5x+3, f(x)) \quad f(x) = 5(1)+3 = 8$  ✓

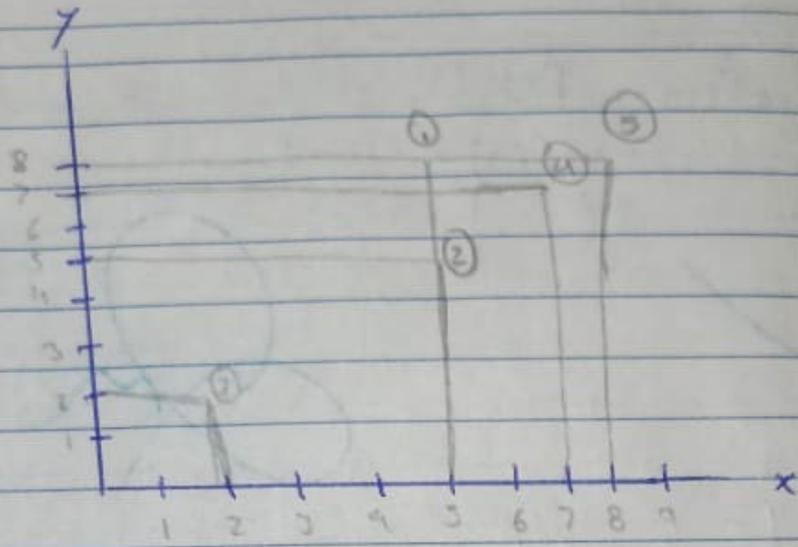
2)  $(x=5x^2, f(x)) \quad f(x) = 5(1)^2 = 5$  ✓

3)  $(x=2x^3, f(x)) \quad f(x) = 2(1)^3 = 2$  ✓

4)  $(x=7x, f(x)) \quad f(x) = 7(1) = 7$  ✓

5)  $(x=8x^2, f(x)) \quad f(x) = 8(1)^2 = 8$  ✓





$f(x) = 2x - 1$

si $f(0)$ $p(0, \quad)$ $x \quad y$	si $f(2)$ $q(2, \quad)$ $x \quad y$
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Traza la grafica  $f(x) =$

si $f(1)$ $p( \quad )$	si $f(3)$ $q( \quad )$
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1)  $f(x) = 3x - 2$

$p = 3(1) - 2$        $q = 3(3) - 2$   
 $p = 3 - 2$        $q = 9 - 2$   
 $p = 1$        $q = 7$

2)  $f(x) = x^2 + 3$

$p = 1^2 + 3$        $q = 3^2 + 3$   
 $p = 1 + 3$        $q = 9 + 3$   
 $p = 4$        $q = 12$   
 $p(1, 4)$

3)  $f(x) = -x + 2$

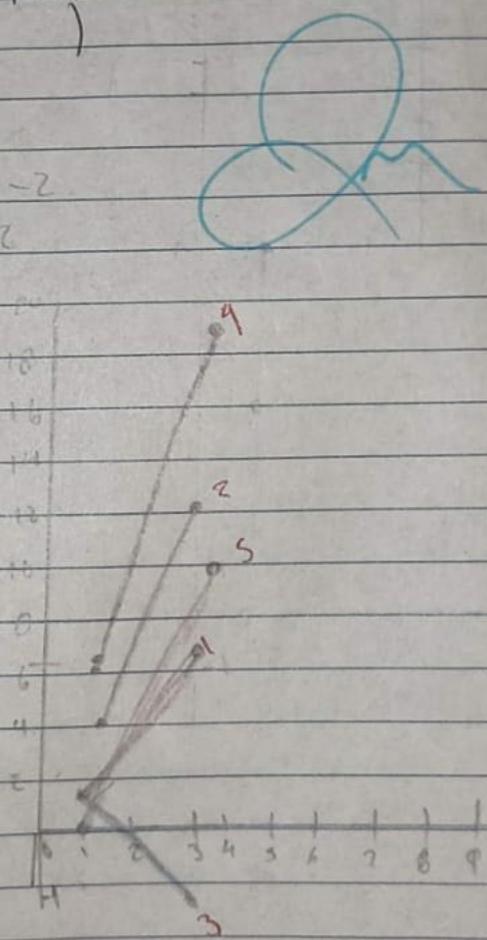
$p = -1 + 2$        $q = -3 + 2$   
 $p = 1$        $q = -1$

4)  $f(x) = 6x + 1$

$p = 6(1) + 1$        $q = 6(3) + 1$   
 $p = 6 + 1$        $q = 18 + 1$   
 $p = 7$        $q = 19$

5)  $f(x) = 5x - 5$

$p = 5(1) - 5$        $q = 5(3) - 5$   
 $p = 5 - 5$        $q = 15 - 5$   
 $p = 0$        $q = 10$



Cultivo  $N_0 \uparrow 50\%$  c/h

Entradas  $N_0 = 2500$  UFC

$$N(t) = N_0 (1.5)^t$$

$$N(1) = N_0 + 0.5 N_0 = N_0 (1.5)^1$$

$$N(2) = N_0 (1.5)^2$$

$$N(3) = N_0 (1.5)^3$$

1) MO  $\uparrow 85\%$  c/h  $\rightarrow$  3hrs y 4 hrs = ✓

$$N_0 + (1.85) = N_0 (1.85)^3 = 6.33 = 15,825$$

$$N_0 + (1.85) = N_0 (1.85)^4 = 11.71 = 29,275$$

2) MO  $\uparrow 60\%$  c/h  $\rightarrow$  1hr y 5hrs ✓

$$N_0 + (0.6) = N_0 (1.6)^1 = 1.6 = 4000$$

$$N_0 + (0.6) = N_0 (1.6)^5 = 10.48 = 26,200$$

3) MO  $\uparrow 20\%$  c/h  $\rightarrow$  1hr y 2hrs ✓

$$N_0 + (0.2) = N_0 (1.2)^1 = 1.2 = 3000$$

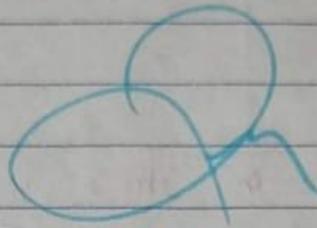
$$N_0 + (0.2) = N_0 (1.2)^2 = 1.44 = 3,600$$

) MO ↑ 35% e/h → 6 hrs / 12 hrs / 24 hrs ✓

$$N_0 + (0.35) = N_0 (1.35)^6 = 6.05 (2500) = 15,125$$

$$N_0 + (0.35) = N_0 (1.35)^{12} = 36.69 (2500) = 91,600$$

$$N_0 + (0.35) = N_0 (1.35)^{24} = 1,342.79 (2500) = 3,356,975$$



Temperatura medida en °C y °F determinada por la igualdad  $9C - 5F + 160 = 0$

Expresa en F °/f de C

$$5F = 9C + 160$$

$$F = \frac{9C + 160}{5}$$

5

$$F = 9/5 C + 32 \rightarrow F(C)$$

Expresa C °/f de F

$$9C = 5F - 160$$

$$C = \frac{5F - 160}{9} \rightarrow C(F)$$

Ej.

38°C

$$F = \frac{9(38) + 160}{5}$$

$$F = \frac{342}{5} + 32 =$$

$$F = 68.4 + 32$$

$$F = 100.4^\circ F$$

$$C = \frac{5(100.4) - 160}{9}$$

$$C = \frac{502 - 160}{9}$$

$$C = \frac{342}{9} = 38^\circ C$$

Convierte de °C a °F o °F a °C

según corresponda y comprueba

1)  $20^{\circ}\text{C}$   $F = \frac{9(20) + 160}{5}$

2)  $104^{\circ}\text{F}$

3)  $140^{\circ}\text{F}$

4)  $37.2^{\circ}\text{C}$

5)  $35.5^{\circ}\text{C}$

6)  $95^{\circ}\text{F}$

7)  $-4^{\circ}\text{F}$

8)  $-5^{\circ}\text{C}$

$C = \frac{5(68) - 160}{9}$

$C = \frac{340 - 160}{9}$

$C = \frac{180}{9} = 20^{\circ}\text{C}$

2)  $C = \frac{5(104) - 160}{9}$

$C = \frac{5(104) - 160}{9} = \frac{520 - 160}{9} = \frac{360}{9} = 40^{\circ}\text{C}$

$F = \frac{9(40) + 160}{5} = \frac{360 + 160}{5} = 104^{\circ}\text{F}$

3)  $C = \frac{5(140) - 160}{9} = \frac{700 - 160}{9} = \frac{540}{9} = 60^{\circ}\text{C}$

$F = \frac{9(60) + 160}{5} = \frac{540 + 160}{5} = \frac{700}{5} = 140^{\circ}\text{F}$

4)  $F = \frac{9(37.2) + 160}{5} = \frac{334.8 + 160}{5} = \frac{494.8}{5} = 98.96^{\circ}\text{F}$

$C = \frac{5(98.96) - 160}{9} = \frac{494.8 - 160}{9} = \frac{334.8}{9} = 37.2^{\circ}\text{C}$

$$5) \quad F = \frac{9(35.5) + 160}{5} = \frac{319.5 + 160}{5} = \frac{479.5}{5} = 95.9^\circ F$$

$$C = \frac{5(95.9) - 160}{9} = \frac{479.5 - 160}{9} = \frac{319.5}{9} = 35.5^\circ C$$

$$6) \quad C = \frac{5(95) - 160}{9} = \frac{315}{9} = 35^\circ C$$

$$F = \frac{9(35) + 160}{5} = \frac{475}{5} = 95^\circ F$$

$$7) \quad C = \frac{5(-9) - 160}{9} = \frac{-20 - 160}{9} = \frac{-180}{9} = -20^\circ C$$

$$8) \quad \frac{9(-5) + 160}{5} = \frac{-45 + 160}{5} = \frac{115}{5} = 23^\circ F$$

