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Ejercicios: A seguir derivando

Biomatemáticas

2° "A"

15 05 22

$F(x) = \frac{\Delta y}{\Delta x}$
 $y = f(x)$
 x_0
 Variable

Derivada de la función en el punto marcado es equivalente a la pendiente de la recta de la tangente.

PH → Variable independiente
 CO² } → Variables dependientes
 O² }

Regla de la derivación

- $f(x) = c$ $f(x) = 7$
 $f'(x) = 0$ $f'(x) = 0$
- $f(x) = x^2$ $f(x) = x^{3+n}$ $n-1=2$
 $f'(x) = P(x^{n-1})$ $f'(x) = 3x^2$
- $f(x) = cx$ $f(x) = 3x^5$ 3×5 $n-1 = 5-1 = 4$
 $f'(x) = c f(x) = c f'(x)$ $15 x^4$
- $f(x) = f \pm g$ $f(x) = 2x^3 \pm x$
 $f'(x) = (f \pm g)' = f' \pm g'$ $f'(x) = 6x^2 \pm 1$
- $f(x) = fg + fg$ $f(x) = (4x+1) + (10x^2-5)$
 $f'(x) = fg' + f'g$ $f'(x) = 20x(4x+1) + 4(10x^2-5)$
- $f(x) = \left(\frac{f}{g}\right) = \frac{fg - fg'}{g^2}$ $f(x) = \frac{4x+1}{10x^2-5}$ $20x(4x+1) - 4(10x^2-5)$

K14

Ejercicios

15 03 22

$X^5 = 5x^4 =$

$X^8 = 8x^7$

$X^9 = 9x^8$

$X^{11} = 11x^{10}$

$X^4 = 4x^3$

$2x^6 = 12x^5$

$4x^2 = 8x$

$5x^3 = 15x^2$

$6x^4 = 24x^3$

$10x^2 = 20x$

Pliny's ball

KUT

Ejercicios

15	03	22
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$4x^3 + 2x = 12x^2 + 2$
 $6x^2 - 3 = 12x$ *constant = 0*
 $2x^4 - x^2 = 8x^3 - 2x$
 $3x^6 + x = 18x^5 + 1$
 $x^7 - 3x = 7x^6 - 3$

A

$(5x^2 + 2) + (3x - 2) = 3(5x^2 + 2) + 10x(3x - 2)$
 $(7x^2 + 2x) + (2x^2 + 5) = 4x(7x^2 + 2x) + 14x(2x^2 + 5)$
 $(2x + 10) - (2x^3 - 10) = 6x^2(2x + 10) - 2(2x^3 - 10)$
 $(6x^4 + 10x) + (6x - 3) = 6(6x^4 + 10x) + 24x^3(6x - 3)$
 $(20x + 2) + (8x^5 + 6) = 40x(20x + 2) - 20(8x^5 + 6)$

Siempre sumamos los términos

KUT

16 03 22

1) $4x^3 + 6x \quad 12x^2 + 6 \quad (4)$

2) $8x^6 \quad f(x) = 48x^5 \quad (3)$

3) $7 \quad f(x) = 0 \quad (1)$ ✓

4) $(3x^3 + 2x) + (6x^4 + 6) \quad f(x) = 24x^3(3x^3 + 2x) + 9x^2(6x^4 + 6) \quad (5)$
 $9x^2 + 2(6x^4 + 6)$

5) $(8x + 2) - (3x^2 - x)$
 $f(x) = 6x(8x + 2) - 8(3x^2 - x) \quad (5)$
 $(6x - 1)(8x + 2) - 8(3x^2 - x)$ ✓

6) $(7x^2 + 4x) + (6x^3 - 2x^2)$
 $18x^2 - 4x(7x^2 + 4x) + 14x + 4(6x^3 - 2x^2)$

7) $(2x^3 - 4x^2) + (2x + x)$
 $2 + 1(2x^3 - 4x^2) + 6x^2 - 8x(2x + x)$

8) $(6x^4 + 2x^5) - (2x^6 + x^3)$
 $12x^3 + 3x^2(6x^4 + 2x^5) - 24x^3 + 10x^4(2x^6 + x^3)$

9) $(3x^3 + 6) - (8x^2 - 2x)$
 $16x - 2(3x^3) - 15x^4(8x^2 - 2x)$

10) $(4x^2 + 3x) + (x^2 + x^2)$
 $3x^2 + 2x(4x^2 + 3x) + 18x + 3(x^2 + x^2)$

Dany Juchelli

Ejercicios



22 08 22

$$f(x) = \frac{5x^2 + 4x}{6x^3} = \frac{18x(5x^2 + 4x) - 10x + 4(6x^3)}{6x^3}$$

$$f(x) = \frac{3x^5 - 7x^4}{2x} = \frac{2(3x^5 - 7x^4) - 15x^4 - 18x^3(2x)}{2x}$$

$$f(x) = \frac{10x^2 + 5x}{15x - 2} = \frac{15(10x^2 + 5x) - 20x + 5(15x - 2)}{(15x - 2)^2}$$

$$f(x) = \frac{2x^{10}}{2x^5} = \frac{10x^4(2x^{10}) - 20x^4(2x^5)}{(2x^5)^2}$$

$$f(x) = \frac{58x}{60x} = \frac{60(58x) - 58(60x)}{(60x)^2}$$



22 03 22

TEOREMA: La derivada de una potencia entera de una función sea

$$y = [f(x)]^n \text{ entonces}$$

$$y' = n [f(x)]^{n-1} f'(x)$$

$f(x) = (2x+3)^2$

$f'(x) = (2)(2x+3)^{2-1} (2)$

$f'(x) = (2)(2x+3)^2 (2)$

$f'(x) = 6(2x+3)^2$

Ejercicios

$f(x) = (3x^4 - 5)^2 = (2)(3x^4 - 5)^{2-1} (12x^3)$
 $(2)(3x^4 - 5)(12x^3)$
 $24x^3(3x^4 - 5)$

$f(x) = (x+2)^3 = (3)(x+2)^{3-1} (1)$
 $3(x+2)^2$

$f(x) = (6x^2 - 5x + 4)^4 = (4)(6x^2 - 5x + 4)^3 (12x - 5)$
 $48x - 20(6x^2 - 5x + 4)^3$

$f(x) = (2xy - 3)^5 = 5(2xy - 3)^{5-1} (2xy)$
 $10(2xy - 3)^4$

$f(x) = (5x^2 + 4y - 3)^2 = 2(5x^2 + 4y - 3)(10x + 4)$
 $20x + 8(5x^2 + 4y - 3)$

TAREA

22 03 22

1. $f(x) = 3x^2 = f(x) = 6x$ ✓
2. $f(x) = 5 = f(x) = 0$ ✓
3. $f(x) = -2x = f(x) = -2$ ✓
4. $f(x) = -2x + 2 = f(x) = -2$ ✓
5. $f(x) = -2x^2 + 2 = f(x) = -4x$ ✓
6. $f(x) = 4x^3 + 6x = f(x) = 12x^2 + 6$ ✓
7. $f(x) = 8x^6 = f(x) = 48x^5$ ✓
8. $f(x) = 7 = f(x) = 0$ ✓
9. $f(x) = (3x^3 + 2x) + (6x^4 + 6) =$
 $f(x) = 24x^3(3x^3 + 2x) + 9x^2 + 2(6x^4 + 6)$ ✓

10. $f(x) = (8x+2) - (3x^2-x)$
 $f(x) = 6x - 1(8x+2) - 8(3x^2-x)$

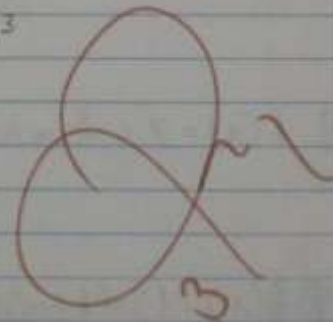
11. $f(x) = (7x^4+6x^3-5x^2+x)^3$
 $f(x) = 3(7x^4+6x^3-5x^2+x)^2 (28x^3+18x^2-10x+1)$
 $84x^2+54x-30+3(7x^4+6x^3-5x^2+x)$

12. $f(x) = \frac{8x^6-6x^3-4}{2x^4}$
 $f(x) = \frac{8x^3(8x^3-6x^3-4) - 48x^3 - 18x^2(2x^4)}{(2x^4)^2}$

13. $f(x) = \frac{2x^3-x^2}{6x^2+x+2}$
 $f(x) = \frac{12x+1(2x^3-x^2) - 6x^2 - 2x(6x^2+x+2)}{(6x^2+x+2)^2}$

14. $f(x) = 78 = f(x) = 0$

15. $f(x) = (2x^3+5x^2+6x)^4$
 $f(x) = 4(2x^3+5x^2+6x)^3 (6x^2+10x+6)$
 $f(x) = 24x+40(2x^3+5x^2+6x)^3$



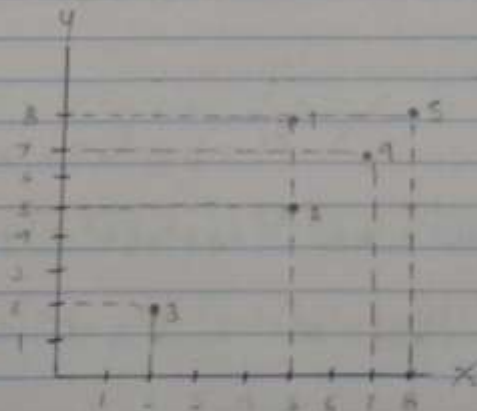
1. $(x=5x+3, f(x)) \quad f(x) = 5(1)+3 = 8$ ✓

2. $(x=5x^2, f(x)) = f(x) = 5(1)^2 = 5$ ✓

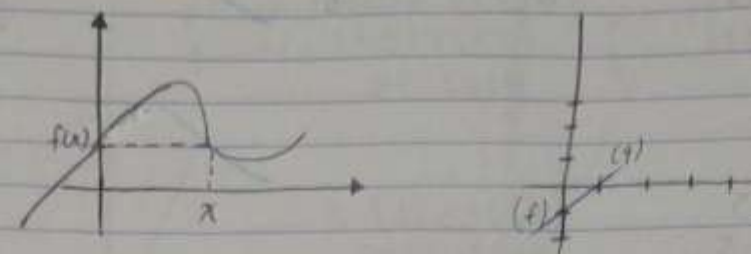
3. $(x=2x^3, f(x)) \quad f(x) = 2(1)^3 = 2$ ✓

4. $(x=7x, f(x)) \quad f(x) = 7(1) = 7$ ✓

5. $(x=8x^2, f(x)) \quad f(x) = 8(1)^2 = 8$ ✓



K/4



Troza la gráfica $f(x) = 2x - 1$

Si $f(0)$	Si $f(1)$
$P(0, -1)$	$q(1, 1)$
$f(0) = 2(0) - 1$	$f(1) = 2(1) - 1$
$f(0) = 0 - 1$	$f(1) = 2 - 1$
$f(0) = -1$	$f(1) = 1$


Ejercicios

Si $f(1)$	Si $f(3)$
$P(1)$	$q(3)$
$P(1, 1)$	$q(3, 7)$ ✓

1. $f(x) = 3x - 2$ $f(3) = 3(3) - 2$
 $f(1) = 3(1) - 2$ $f(3) = 9 - 2$
 $f(1) = 1$ $f(3) = 7$

2. $f(x) = x^2 + 3$ $f(3) = 3^2 + 3$ ✓
 $f(1) = 1^2 + 3$ $f(3) = 9 + 3$
 $f(1) = 1 + 3$ $f(3) = 12$
 $f(1) = 4$

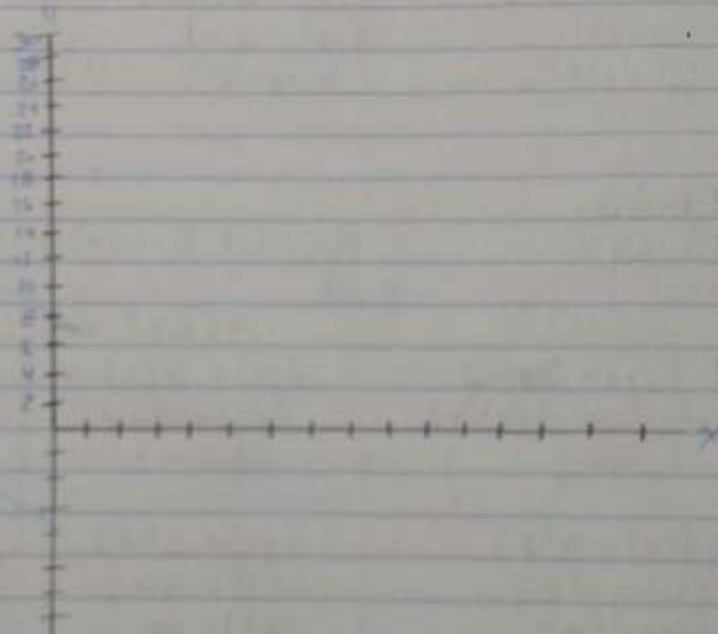
3. $f(x) = -x + 2$ $f(3) = -3 + 2$ ✓
 $f(1) = -1 + 2$ $f(3) = -1$
 $f(1) = 1$

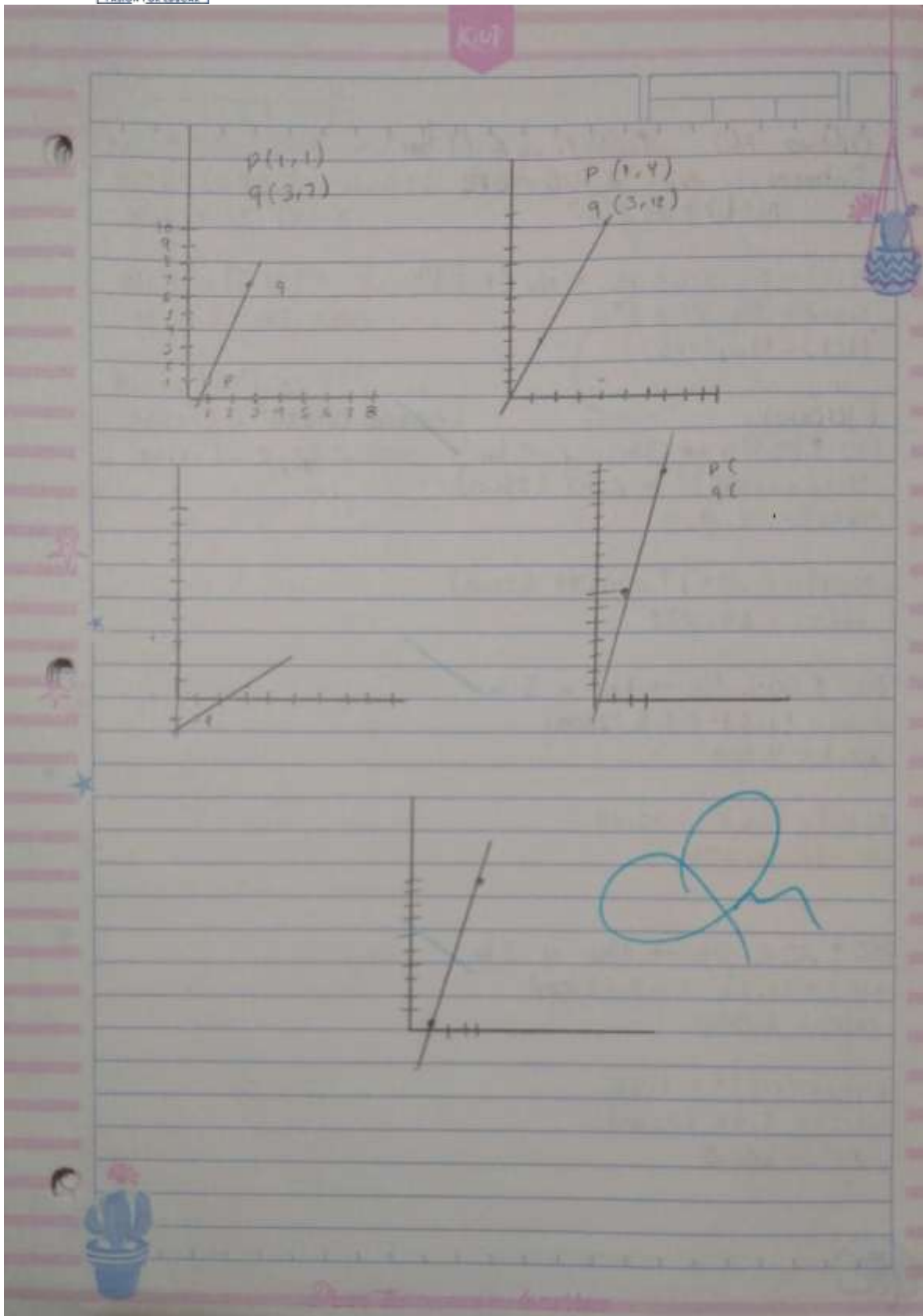


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4. $f(x) = 6x + 1$ $f(3) = 6(3) + 1$
 $f(1) = 6(1) + 1$ $f(3) = 18 + 1$
 $f(1) = 6 + 1$ $f(3) = 19$
 $f(1) = 7$

5. $f(x) = 5x - 5$ $f(3) = 5(3) - 5$
 $f(1) = 5(1) - 5$ $f(3) = 15 - 5$
 $f(1) = 5 - 5$ $f(3) = 10$
 $f(1) = 0$





Cultivo MO ↑ 50% c/h

Entonces... $N_0 = 2500$ UFC

$$N(t) = N_0 (1.5)^t$$

$$N(1) = N_0 \cdot 1.5 N_0 = N_0 (1.5)^1$$

$$N(2) = N_0 (1.5)^2$$

$$N(3) = N_0 (1.5)^3$$

Ejercicios

MO ↑ 85% c/h → 3 hrs y 4 hrs

$$N(3) = (1.85)^3 = 6.33 (2500)$$

$$N(3) = 15,825$$

$$N(4) = (1.85)^4 = 11.71 (2500)$$

$$N(4) = 29,275$$

MO ↑ 60% c/h → 1 hr y 5 hr

$$N(1) = (1.6)^1 = 1.6 (2500)$$

$$N(1) = 4,000$$

$$N(5) = (1.6)^5 = 10.48$$

$$N(5) = 26,200$$

MO ↑ 20% c/h → 1 hr y 2 hr

$$N(1) = (1.2)^1 = 1.2 (2500)$$

$$N(1) = 3,000$$

$$N(2) = (1.2)^2 = 1.44$$

$$N(2) = 1.44 (2500)$$

$$N(2) = 3,600$$

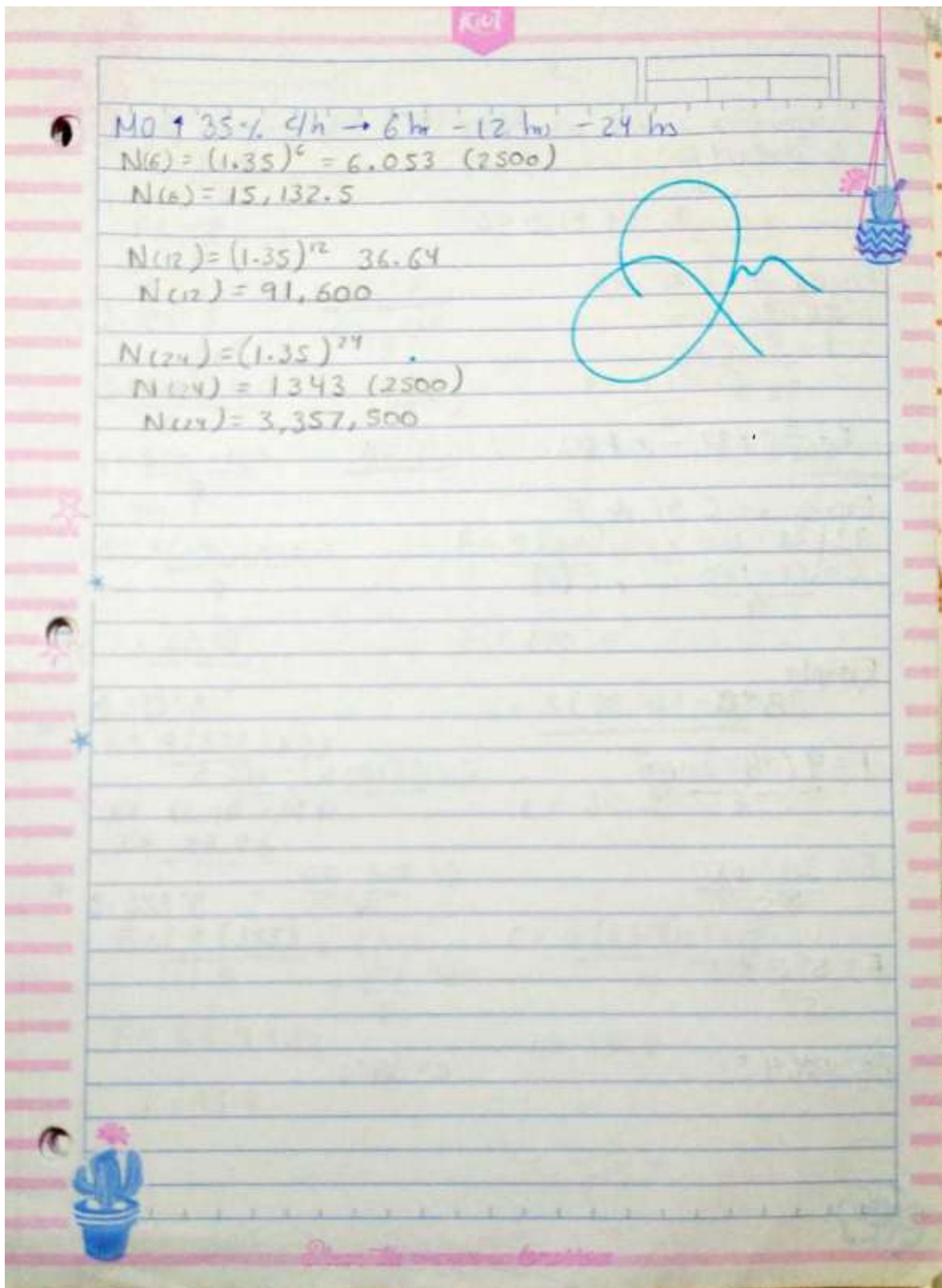


KOL

$M0 \uparrow 35\% \text{ c/h} \rightarrow 6 \text{ hr} - 12 \text{ hr} - 24 \text{ hr}$
 $N(6) = (1.35)^6 = 6.053 \text{ (2500)}$
 $N(6) = 15,132.5$

$N(12) = (1.35)^{12} = 36.64$
 $N(12) = 91,600$

$N(24) = (1.35)^{24} = 1343 \text{ (2500)}$
 $N(24) = 3,357,500$



K4

1. 20°C $F = \frac{9}{5}(C) + 32$

$$F = \frac{9(20)}{5} + 32$$

$$F = \frac{180}{5} + 32$$

$$F = 36 + 32 = 68^{\circ}\text{F}$$

2. 104°F $C = \frac{5}{9}(F) - 160$

$$C = \frac{5(104) - 160}{9}$$

$$C = \frac{520 - 160}{9}$$

$$C = \frac{360}{9} = 40^{\circ}\text{C}$$

3. 140°F $F = \frac{9}{5}(C) + 32$

$$C = \frac{5(140) - 160}{9}$$

$$C = \frac{700 - 160}{9}$$

$$C = \frac{540}{9} = 60^{\circ}\text{C}$$

4. 372°C $C = \frac{5}{9}(F) - 160$

$$F = \frac{9(372)}{5} + 32$$

$$F = 66.96 + 32$$

$$F = 98.96$$

5. 355°C $C = \frac{5}{9}(F) - 160$

$$F = \frac{9(355)}{5} + 32$$

$$F = 63.9 + 32$$

$$F = 95.9$$

Dios te muestre sus caminos

K.01

6. 95°F
 $C = \frac{5(95) - 160}{9}$
 $C = 35$

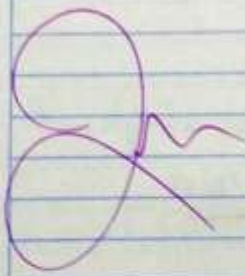





$F = \frac{9(35)}{5} + 32$
 $F = 95$

7. -4°F
 $C = \frac{5(-4) - 160}{9}$
 $C = -20$

$F = \frac{9(-20)}{5} + 32$
 $F = -4$

8. -5°C
 $F = \frac{9(-5)}{5} + 32$
 $F = 23$

$C = \frac{5(23) - 160}{9}$
 $C = -5$

University of the Pacific