

Nombre de la actividad: Derivadas

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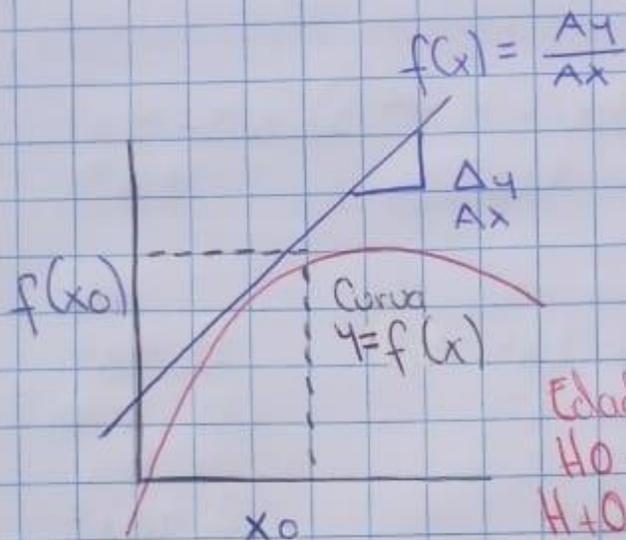
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Materia: Biomatemáticas

Grado: 2

Grupo: A

Derivadas.



Edad → Variable independiente
 H₂O → } Variable dependiente.
 H₂O → }

Derivadas de la función en el punto marcado es equivalente a la pendiente de la recta de la tangente.

PH → Variable independiente
 CO₂ → } Variable dependiente
 O₂ → }

Reglas de la derivación

① $f(x) = C$
 $f'(x) = 0$
 $f(x) = 7$
 $f'(x) = 0$

② $f(x) = x^n$
 $f'(x) = nx^{n-1}$
 $f(x) = x^3$
 $f'(x) = 3x^2$

③ $f(x) = cx$ $f(x) = 3x^5$
 $f'(x) = c$ $f'(x) = 15x^4$

④ $f(x) = f \pm g$
 $f'(x) = (f \pm g)' = f' \pm g'$
 $f(x) = 2x^3 \pm x$
 $f'(x) = 6x^2 \pm 1$

⑤ $f(x) = f \cdot g$
 $f'(x) = f'g + fg'$

$f(x) = 3x^5$
 $f'(x) = 15x^4$

$f(x) = (4x+1)(10x^2-5)$
 $f'(x) = 20x(4x+1) + 4(10x^2-5)$

$$f(x) = x^n$$

$$f'(x) = nx^{n-1}$$

Ejercicios

$$1) x^5 = 5x^4 \quad 2) x^8 = 8x^7 \quad 3) x^4 = 4x^3$$

$$5x^4 \quad 8x^7 \quad 4x^3$$

$$4) x^{11} = 11x^{10} \quad 5) x^4 = 4x^3$$

$$11x^{10} \quad 4x^3$$

$$f(x) = cx$$

$$f'(x) = cf(x) = cf'(x)$$

Ejercicios

$$1) 2x^6$$

$$f(x) = 2(2x^6)$$

$$f(x) = 4x^6$$

$$2) 4x^2$$

$$f(x) = 4(4x^2)$$

$$f(x) = 16x^2$$

$$3) 5x^3$$

$$f(x) = 5(5x^3)$$

$$f(x) = 25x^3$$

$$4) 6x^4$$

$$f(x) = 6(6x^4)$$

$$f(x) = 36x^4$$

$$5) 10x^2$$

$$f(x) = 10(10x^2)$$

$$f(x) = 100x^2$$

Ejercicios

$$f(x) = f \pm g$$

$$f'(x) = (f \pm g)' = f' \pm g'$$

$$1) 4x^3 + 2x$$

$$f(x) = 12x^2 + 2x$$

$$2) 6x^2 - 3$$

$$f(x) = 6x^2 - 3$$

$$f'(x) = 12x$$

$$3) 2x^4 - x^2$$

$$f(x) = 8x^3 - 2x$$

$$4) 3x^6 + x$$

$$f(x) = 18x^5 + 1$$

$$5) x^7 - 3x$$

$$f(x) = 7x^6 - 3$$

$$f(x) = fg + fg$$
$$f'(x) = fg' + f'g.$$



Ejercicios

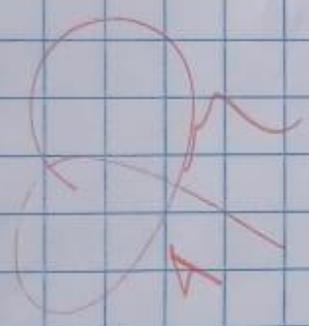
1) $(5x^2 + 2) + (3x - 2)$
 $3x(5x^2 + 2) + 5(3x - 2)$

2) $(7x^3 + 2x) + (2x^2 + 5x)$
 $4x(7x^3 + 2x) + 7(2x^2 + 5x)$

3) $(2x + 10) - (2x^3 - 10)$
 $-6x(2x + 10) - 2(2x^3 - 10)$

4) $(8x^4 + 10x) + (6x - 3)$
 $6x(8x^4 + 10x) + 8(6x - 3)$

5) $(20x + 2) - (8x^5 + 6)$
 $40x(20x + 2) - 20(8x^5 + 6)$



16-03-2022

Biomatemáticas

① $4x^3 + 6x$
 $12x^2 + 6$

② $8x^6$
 $8(6x^5)$

③ 7
 $f(x) = 0$ Regla 11

Regla 4
④ $(3x^3 + 2x) + (6x^4 + 6)$ Reglas 3
 $24x^3 + 3x^3 + 9x^4 + 6x^4 + 6$ Reglas 5

⑤ $(8x + 2) - (3x^2 - x)$ Reglas 5
 $6x - 1(8x + 2) - 8(3x^2 - x)$

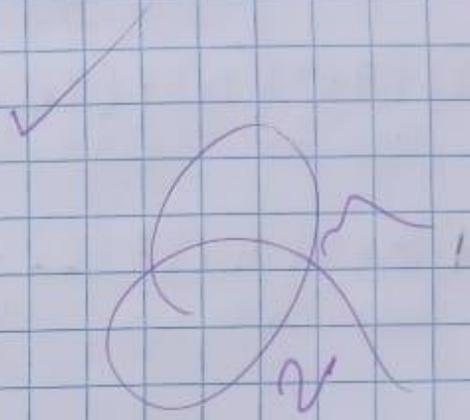
⑥ $(7x^2 + 4x) + (6x^3 - 2x^2)$
 $18x^2 + 4x(7x^2 + 4x) + 14x + 4x(6x^3 - 2x^2)$

⑦ $(2x^3 - 4x^2) + (2x + x)$
 $24(2x^3 - 4x^2) + 6x^2 - 8x(2x + x)$

⑧ $(6x^4 + 2x^5) - (2x^6 + x^5)$
 $17x^3 + x^5(6x^4 + 2x^5) - 74x^3 + 10x^4(2x^6 + x^5)$

⑨ $(3x^5 + 6) - (8x^2 - 2x)$
 $16x - 2(3x^5 + 6) - 15x^4 + 6(8x^2 - 2x)$

⑩ $(9x^2 + 3x) + (x^3 + x^2)$
 $3x^2 + 2x(9x^2 + 3x) + 18x + 3x(x^3 + x^2)$



22/03/2022
Martes.

$$6) f(x) \left| \frac{f}{g} \right| f'(x) = \frac{f'g - fg'}{g^2}$$

Ejemplo.

$$f(x) \frac{4x+1}{10x^2-5} \quad \frac{20x(4x+1) - 4(10x^2-5)}{(10x^2-5)^2}$$

Ejercicios.

$$① f(x) \frac{5x^2+4x}{6x^3} \quad \frac{18x^2(5x^2+4x) - (10x+4)(6x^3)}{6x^3}$$

$$② f(x) \frac{3x^5-7x^4}{2x} \quad \frac{2(3x^5-7x^4) - (15x^4-18x^3)(2x)}{(2x)^2}$$

$$③ f(x) \frac{10x^2+5x}{15x-2} \quad \frac{15(10x^2+5x) - 20x+5}{(15x-2)^2}$$

$$④ f(x) \frac{2x^{10}}{2x^5} \quad \frac{10x^4(2x^{10}) - 20x^9(2x^3)}{(2x^5)^2}$$

$$⑤ f(x) \frac{58x}{60x} \quad \frac{60(58x) - 58(60x)}{60x}$$

TEOREMA:

La derivada de 1 potencia entera de 1 función sea:

$$y = [f(x)]^n \text{ entonces}$$

$$y' = n [f(x)]^{n-1} f'(x)$$

Ejemplo.

$$f(x) = (2x+3)^3$$
$$f'(x) = (3)(2x+3)^{3-1} (2)$$
$$f'(x) = (3)(2x+3)^2 (2)$$
$$f'(x) = 6(2x+3)^2$$

Ejercicios.

① $f(x) = (3x^4 - 5)^2$ ✓

$$f'(x) = (2)(3x^4 - 5)^{2-1} (12x^3)$$
$$f'(x) = (2)(3x^4 - 5)^1 (12x^3)$$
$$f'(x) = 24x^3 (3x^4 - 5)$$

④ $f(x) = (2x^4 - 3)^5$ ✓

$$f'(x) = 10(2x^4 - 3)^4$$

② $f(x) = (x+2)^3$ ✓

$$f'(x) = 3(x+2)^2$$

⑤ $f(x) = (5x^2 + 4y - 3)^2$ ✓

$$f'(x) = 20x + 8(5x^2 + 4y - 3)$$

③ $f(x) = (6x^2 - 5x + 4)^4$ ✓

$$f'(x) = 48x - 20(6x^2 - 5x + 4)^3$$

Biomatemáticas

Ejercicios Tarea

$$\textcircled{1} f(x) = 3x^2 = 6x \quad \checkmark$$

$$\textcircled{2} f(x) = 5 = \emptyset \quad \checkmark$$

$$\textcircled{3} f(x) = -2 \quad \checkmark$$

$$\textcircled{4} f(x) = -2x + 2 = -2 \quad \checkmark$$

$$\textcircled{5} f(x) = -2x^2 + 2 = -4x \quad \checkmark$$

$$\textcircled{6} f(x) = 4x^3 + 6x = 2x^2 \quad \checkmark$$

$$\textcircled{7} f(x) = 8x^6 = 48x^5 \quad \checkmark$$

$$\textcircled{8} f(x) = 7 = \emptyset \quad \checkmark$$

$$\textcircled{9} f(x) = (3x^3 + 2x) + (6x^4 + 6) \quad \checkmark$$

$$24x^3(3x^3 + 2x) + 9x^6 + 2(6x^4 + 6)$$

$$\textcircled{10} f(x) = (8x + 2) - (3x^2 - x) \quad \checkmark$$

$$6x - 1(8x + 2) - 8(3x^2 - x)$$

$$\textcircled{11} f(x) = (7x^4 + 6x^3 - 5x^2 - x)^3 = \quad \checkmark$$

$$(3)(7x^4 + 6x^3 - 5x^2 - x)^2 (28x^3 + 5x^2) - (3)(7x^4 + 6x^3 - 5x^2 - x)^2$$

$$84x^3 + 54x^2 - 30x - 3(7x^4 + 6x^3 - 5x^2 - x)^2$$

Biomatemáticas.

Biomatemáticas. Biomatemáticas

$$(12) f(x) \frac{8x^6 - 6x^3 - 4}{2x^4} \quad \checkmark \quad \frac{8x^5 (8x^6 - 6x^3 - 4) - 48x^5 - 18x^3 (2x^4)}{(2x^4)^2}$$

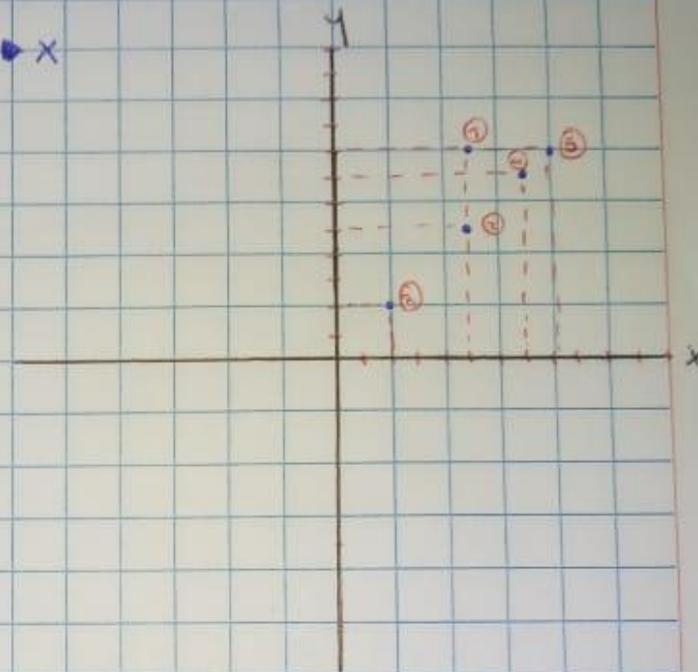
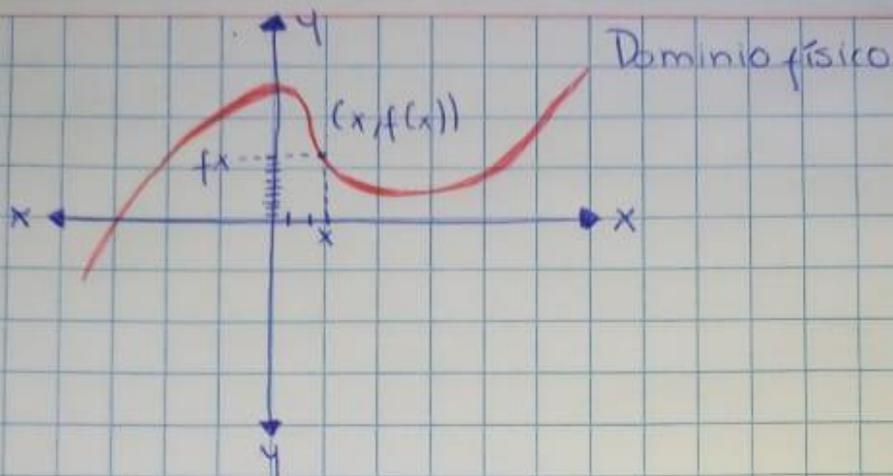
$$(13) f(x) \frac{2x^3 - x^2}{6x^2 + x + 2} \quad \checkmark \quad \frac{2x + 4(2x^3 - x^2) - 6x^2 - 2x(6x^2 + x + 2)}{(6x^2 + x + 2)^2}$$

$$(14) f(x) = 78 \quad \emptyset \quad \checkmark$$

$$(15) f(x) = (2x^3 + 5x^2 + 6x)^4 \quad \checkmark$$

$$24(2x^3 + 5x^2 + 6x)^3 (6x^2 + 10x + 6)$$
$$24x^2 + 40x + 24(2x^3 + 5x^2 + 6x)^3$$

3



Ejemplo.

$$f(x) = 3x$$

$$y = 3x$$

Ejercicios.

① $(x = 5x + 3, f(x))$ ✓
 $y = 8$

④ $(x = 7x, f(x))$ ✓
 $y = 7(1)$
 $y = 7$

② $(x = 5x^2, f(x))$ ✓
 $y = 5(x)^2$
 $y = 5(1) = 5$

⑤ $(x = 8x^2, f(x))$ ✓
 $y = 8(x)^2$
 $y = 8(1) = 8$

③ $(x = 2x^3, f(x))$ ✓
 $y = 2(x)^3$
 $y = 2(1) = 2$

