



**Derivadas**

**Biomatemáticas**

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**2° A**

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PASIÓN POR EDUCAR

$$f(x) = x^2$$

$$f'(x) = n x^{n-1}$$

regla 2

- 1)  $x^5 =$
- 2)  $x^8 =$
- 3)  $x^9 =$
- 4)  $x^{11} =$
- 5)  $x^4 =$

- 1)  $f(x) = x^5$
- $f'(x) = 5x^4$
- $f(x) = 9x$

ejercicio n.3

- 1)  $2x^6 = 12x^5$
- 2)  $9x^2 = 9x$
- 3)  $5x^3 = 15x^2$
- 4)  $6x^4 = 24x^3$
- 5)  $10x^2 = 20x$

ejemplo

$$f(x) = 3x^5$$

$$f'(x) = 3(5x^4)$$

$$15x^4$$

- 1)  $f(x) = 2x^6$
- $f'(x) = 2(6x^5)$
- $12x^5$

ejercicio regla 4

- 1)  $4x^3 + 2x = 12x^2 + 2$
- 2)  $6x^2 - 3 = 12x$
- 3)  $2x^4 - x^2 = 8x^3 - 2x$
- 4)  $3x^6 + x = 18x^5 + 1$
- 5)  $x^4 - 3x = 7x^3 - 3$

ejemplo:

$$f(x) = 2x^3 + x$$

$$f'(x) = 6x^2 + 1$$

- 1)  $12x^2 + 2$

- 2)  $12x - 3$  — por la primera regla se elimina
- $12x$  — se elimina

(no hay  $Cx$  se elimina)

ejercicios regla 5

$$1) (5x^2 + 2) + (3x - 2) =$$

$$3(5x^2 + 2) + 10x(3x - 2)$$

ejemplo

$$f(x) = (4x + 1)(10x^2 - 5)$$

$$f'(x) = 20x(4x + 1) + 4(10x^2 - 5)$$

$$2) (7x^3 + 2x) + (2x^2 + 5x) =$$

$$4x(7x^3 + 2x) + 2x(2x^2 + 5x)$$

✓

$$3) (2x + 10) - (2x^3 - 10) =$$

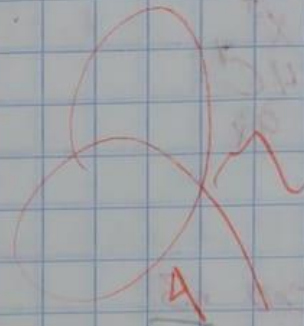
$$6x^2(2x + 10) - 2(2x^3 - 10)$$

$$4) (8x^4 + 10x) + (6x - 3) =$$

$$6(8x^4 + 10x) + 32(6x - 3)$$

$$5) (20x + 2) - (8x^5 + 6) =$$

$$40x^4(20x + 2) - 20(8x^5 + 6)$$



16/03/22

1)  $4x^3 + 6x$  ✓  
 $12x^2 + 6$  ✓

Regla 4  
 $f(x) = f + g$   
 $f'(x) = (f + g)' = f' + g'$

2)  $8x^6$  ✓  
 $8(6x^5)$  ✓  
 $48x^5$  ✓

Formula Regla 2  
 $f(x) = x^2$   
 $f'(x) = nx^{n-1}$

3) 7 ✓  
 $f(x) = 7$  ✓  
 $f'(x) = 0$  ✓

Regla 1  
 $f(x) = C$   
 $f'(x) = 0$

4)  $(3x^5 + 2x) + (6x^4 + 6)$  ✓  
 $24x^3(3x^3 + 2x) + 9x^2(6x^4 + 6)$  ✓

Regla 5  
 $f(x) = fg + fg$   
 $f'(x) = f'g + fg'$

5)  $(8x + 2) - (3x^2 - x)$  ✗  
 $6x(8x + 2) - 8(3x^2 - x)$  ✗

Regla 5

↓  
 $6x - 1(8x + 2) - 8(3x^2 - x)$  ✓

$$6) (7x^2 + 4x) + (6x^3 - 2x^2)$$

$$8x^2 - 4x(7x^2 + 4x) + 14x + 4(6x^3 - 2x^2)$$

$$7) (2x^3 - 4x^2) + (2x + x)$$

$$2 + 1(2x^3 - 4x^2) + 6x^2 - 8x(2x + x)$$

$$8) (6x^4 + 2x^5) - (2x^6 + x^3)$$

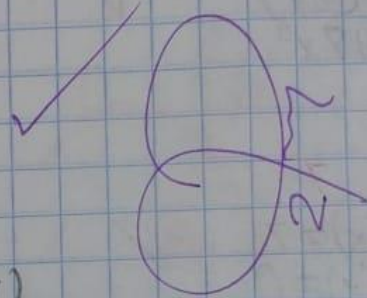
$$12x^5 - 5(6x^4 + 2x^5) - 24x^6 + 10x^3(2x^6 + x^5)$$

$$9) (3x^5 + 6) - (8x^2 - 2x)$$

$$16x - 2(3x^5 + 6) - 15x^4(8x^2 - 2x)$$

$$10) (9x^2 + 3x) + (x^3 + x^2)$$

$$3x^2 + 2x(9x^2 + 3x) + 18x + 3(x^3 + x^2)$$



22/03/2023

Formula fo

$$a) f(x) = (fg)' \quad f'(x) = fg' \pm f'g$$

$$b) f(x) = \left[ \frac{f}{g} \right] \quad f'(x) = \frac{fg' - f'g}{g^2}$$

Ej

$$f(x) = \frac{4x+1}{10x^2-5} = \frac{20x(4x+1) - 4(10x^2-5)}{(10x^2-5)^2}$$

Ejercicios

$$1) f(x) = \frac{5x^2 + 4x}{6x^3} = \frac{18x^2(5x^2 + 4x) - (10x+4)(6x^3)}{(6x^3)^2}$$

$$2) f(x) = \frac{3x^5 - 7x^9}{2x} = \frac{2(3x^5 - 7x^9) - (15x^4 - 28x^3)(2x)}{(2x)^2}$$

$$3) f(x) = \frac{10x^2 + 8x}{15x - 2} = \frac{15x(10x^2 + 8x) - (20x + 8)(15x - 2)}{(15x - 2)^2}$$

$$4) f(x) = \frac{2x^{10}}{2x^5} = \frac{10x^9(2x^{10}) - (20x^9)(2x^5)}{(2x^5)^2}$$

$$5) f(x) = \frac{88x}{60x} = \frac{60(88x) - (88)(60x)}{(60x)^2}$$

Teorema: La derivada de 1 potencia entera de 1 sea  $y = [f(x)]^n$  entonces:  
 $y' = n[f(x)]^{n-1} f'(x)$

Ejemplo

$$f(x) = (2x+3)^3$$

$$f'(x) = (3)(2x+3)^{3-1}(2)$$

$$f'(x) = (3)(2x+3)^2(2)$$

$$f'(x) = 6(2x+3)^2$$

Ejercicios

1)  $f(x) = (3x^4 - 5)^2$

$$f'(x) = (2)(3x^4 - 5)^{2-1}(12x^3)$$

$$f'(x) = (2)(3x^4 - 5)(12x^3)$$

$$f'(x) = (24x^3)(3x^4 - 5)$$

2)  $f(x) = (x+2)^3$

$$f'(x) = (3)(x+2)^{3-1}(1)$$

$$f'(x) = (3)(x+2)^2(1)$$

$$f'(x) = (3)(x+2)^2$$

3)  $f(x) = (6x^2 - 5x + 4)^4$

$$f'(x) = (4)(6x^2 - 5x + 4)^{4-1}(12x - 5)$$

$$f'(x) = (48x - 20)(6x^2 - 5x + 4)^3$$

4)  $f(x) = (2xy - 3)^5$

$$f'(x) = (5)(2xy - 3)^{5-1}(2y)$$

$$f'(x) = 10(2xy - 3)^4$$

Cultivo MO ↑ 50% c/hr  
 enforces  $N_0 = 2500$  v/c  
 $NCE) = NCE)^h$

$$NCE) = N_0 + 0.5 N_0 = N_0 (1.5)^h$$

$$NCE) = N_0 (1.5)^2$$

$$NCE) = N_0 (1.5)^3$$

1) MO ↑ 85% / hr → 3 hrs y 4 hrs

$$NCE) = N_0 (0.85) N_0 = N_0 (1.85)^h$$

$$NCE) = N_0 (0.85)^3 = 2500 (1.85)^3$$

$$= 2500 (6.33)$$

$$= 15,825 \text{ v/c}$$

$$NCE) = N_0 (0.85)^4 = 2500 (1.85)^4$$

$$= 2500 (11.71)$$

$$= 29,275$$

2) MO ↑ 60% c/h → 1 hr y 5 hrs

$$NCE) = N_0 (0.6) N_0 = N_0 (1.6)^h$$

$$NCE) = N_0 (1.6)^2 = 2500 (1.6)$$

$$= 4000$$

$$NCE) = N_0 (1.6)^5 = 2500 (1.6)^5$$

$$= 2500 (10.48)$$

$$= 26,200$$

3) MO ↑ 20% c/h → 1 hr y 2 hrs

$$NCE) = N_0 (1.2)^1 = 2500 (1.2)$$

$$= 3000$$

$$NCE) = N_0 (1.2)^2 = 2500 (1.2)^2$$

$$= 2500 (1.44)$$

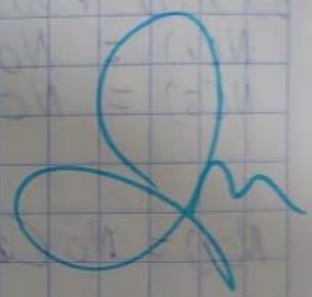
$$= 3600$$



4) MO  $\uparrow$  35%  $\%n \rightarrow$  6 hrs / 12 hrs / 24 hrs

$$N(6) = (1.35)^6 = 2800 (1.35)^6 \\ = 2800 (6.68) \\ = 18,125$$

$$N(12) = (1.35)^{12} = 2800 (1.35)^{12} \\ = 2800 (36.64) \\ = 102,792$$



Convertir de  $^{\circ}\text{C}$  a  $^{\circ}\text{F}$  o  $^{\circ}\text{F}$  a  $^{\circ}\text{C}$   
Según corresponda y comprobar

1)  $20^{\circ}\text{C}$

$$9(20) + 32$$

$$\frac{180 + 32}{5} = 68^{\circ}\text{F}$$

2)  $104^{\circ}\text{F}$

$$5(104) - 160$$

$$520 - 160 = \frac{360}{9} = 40^{\circ}\text{C}$$

3)  $140^{\circ}\text{F}$

$$5(140) - 160$$

$$700 - 160$$

$$\frac{540}{9} = 60^{\circ}\text{C}$$

4)  $37.2^{\circ}\text{C}$

$$9(37.2) + 32$$

$$\frac{334.8 + 32}{5} = 98.96^{\circ}\text{F}$$

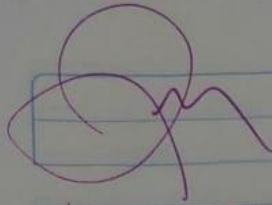
$$66.96 + 32 =$$

5)  $35.5^{\circ}\text{C}$

$$9(35.5) + 32$$

$$\frac{319.5 + 32}{5} = 90.9^{\circ}\text{F}$$

$$63.9 + 32 = 95.9^{\circ}\text{F}$$



6) 95 °F

$$S(95) - 160$$

$$475 - 160 = \frac{315}{9} = 35 \text{ °C}$$

7) 40 °F

$$S(-4) - 160 = \frac{-180}{9} = -20 \text{ °C}$$

8) 50 °F

$$9(-5) + 32$$

$$\frac{(-45) + 32}{5} = 23 \text{ °F}$$