

CALCULO INTEGRAL

Ola grupo ☺

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$$\int x^4 dx = \frac{4x^{4+1}}{4+1} = \frac{4x^5}{5} + C$$

$$y = \frac{4x^5}{5} = \frac{20x^{5-1}}{5} = \frac{4x^4}{5}$$

FORMULA

$$x^n dx \Rightarrow \frac{x^{n+1}}{n+1} + C$$

A)  $\int 3x^4 dx = \frac{3x^{4+1}}{4+1} = \frac{3x^5}{5} + C$

B)  $\int 2x^7 dx = \frac{2x^{7+1}}{7+1} = \frac{2x^8}{8} + C = \frac{x^8}{4} + C$

C)  $\int \frac{1}{x^3} dx = \int x^{-3} dx = \frac{x^{-3+1}}{-3+1} = \frac{x^{-2}}{-2} = -\frac{1}{2x^2} + C$

D)  $\int \frac{1}{x^5} dx = \int x^{-5} dx = \frac{x^{-5+1}}{-5+1} = \frac{x^{-4}}{-4} = -\frac{1}{4x^4} + C$

E)  $\int \frac{3}{5} x^6 dx = \frac{3}{5} \int x^6 dx = \frac{3}{5} \cdot \frac{x^{6+1}}{6+1} = \frac{3 \cdot x^7}{5 \cdot 7} = \frac{3x^7}{35} + C$

F)  $\int \frac{3}{t^5} dt = 3 \int t^{-5} dt = 3 \cdot \frac{t^{-5+1}}{-5+1} = \frac{3t^{-4}}{-4} = -\frac{3}{4t^4} + C$

G)  $\int 5u^{3/2} du = 5 \int u^{3/2} du = 5 \cdot \frac{u^{3/2+2/2}}{3/2+2/2} = 5 \cdot \frac{u^{5/2}}{5/2} = \frac{10u^{5/2}}{5} = 2u^{5/2} + C$

$$H) \int 10 \sqrt[3]{x^2} dx = \int 10 x^{2/3} dx = 10 \int x^{2/3} dx =$$

$$10 \cdot \frac{x^{2/3+3/3}}{2/3+3/3} = \frac{10 \cdot x^{5/3}}{5/3} = \frac{30 x^{5/3}}{5} = \underline{6x^{5/3} + C}$$

$$I) \int \frac{2}{3\sqrt{x}} dx = \int 2x^{-1/3} dx = \frac{2 \cdot x^{-1/3+3/3}}{-1/3+3/3} = \frac{2 \cdot x^{2/3}}{2/3} = \frac{6x^{2/3}}{2} = \underline{3x^{2/3} + C}$$

$$t^2 = 6/3 + 1/3 + t$$

$$J) \int 6t^2 \sqrt[3]{t} dt = \int 6t^2 t^{1/3} dt = \int 6t^{7/3} dt =$$

$$6 \int t^{7/3} dt = \frac{6 \cdot t^{7/3+3/3}}{7/3+3/3} = \frac{6t^{10/3}}{10/3} = \frac{18t^{10/3}}{10} = \underline{9/5 t^{10/3} + C}$$

$$K) \int 7x^3 \sqrt{x} dx = \int 7x^3 x^{1/2} dx = 7 \int x^{7/2} dx = 7 \int x^{3.5} dx =$$

$$\frac{7 \cdot x^{7/2+1/2}}{7/2+1/2} = \frac{7x^4}{9} = \underline{\frac{14x^4}{9} + C}$$

$$L) \int 4x^3 + x^2 dx = 4 \int x^3 dx = \frac{4 \cdot x^{3+1}}{3+1} = \frac{4x^4}{4} = \underline{x^4}$$

$$\int x^2 = \frac{x^{2+1}}{2+1} = \frac{x^3}{3} \Rightarrow \underline{x^4 + \frac{x^3}{3} + C}$$

$$M) \int 3u^5 - 2u^3 dx = 3 \int u^5 dx = \frac{3 \cdot u^{5+1}}{5+1} = \frac{3u^6}{6} = \underline{\frac{u^6}{2}}$$

$$2 \int u^3 = \frac{2 \cdot u^{3+1}}{3+1} = \frac{2u^4}{4} = \frac{u^4}{2} \Rightarrow \underline{\frac{u^6}{2} - \frac{u^4}{2} + C}$$

$$N) \int y^3 (2y^2 - y) dy$$

$$\int 2y^5 - y^4 = 2 \int y^5 = \frac{2 \cdot y^{5+1}}{5+1} = \frac{2y^6}{6} = \underline{\frac{y^6}{3}}$$

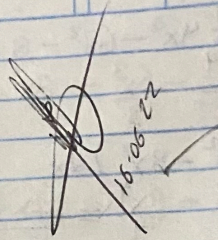
$$\int y^4 = \frac{y^{4+1}}{4+1} = \frac{y^5}{5} =$$

$$\underline{\frac{y^6}{3} - \frac{y^5}{5} + C}$$

$$o) \int x^4 (5-x^2) dx \quad \int 5x^4 - x^6 =$$

$$\frac{5 \cdot x^{4+1}}{4+1} - \frac{x^7}{7} = x^5 - \frac{x^7}{7} + C$$

$$\frac{x^{6+1}}{6+1} = \frac{x^7}{7}$$



$$p) \int (3-2t+t^2) dt$$

$$3t - 2t + t^2 = \frac{3t^{1+1}}{1+1} - \frac{2t^{1+1}}{1+1} + \frac{t^{2+1}}{2+1} = \frac{3t^2}{2} - t^2 + \frac{t^3}{3} + C$$

$$q) \int \sqrt{x} (x+1) dx =$$

$$x^{\frac{1}{2}} (x+1) dx = \frac{x^{\frac{3}{2}}}{\frac{3}{2}} + \frac{x^{\frac{1}{2}}}{\frac{1}{2}}$$

$$= \frac{2x^{\frac{3}{2}}}{3} + \frac{2x^{\frac{1}{2}}}{1} + C$$

$$\frac{x^{\frac{3}{2}+2}}{\frac{3}{2}+2} = \frac{x^{\frac{5}{2}}}{\frac{5}{2}} = \frac{2x^{\frac{5}{2}}}{5}$$

$$\frac{x^{\frac{1}{2}+2}}{\frac{1}{2}+2} = \frac{x^{\frac{3}{2}}}{\frac{3}{2}} = \frac{2x^{\frac{3}{2}}}{3}$$

R)  $\int (8x^4 + 4x^3 - 6x^2 - 8) dx$  ← Directo  
 $\frac{8x^5}{5} + \frac{4x^4}{4} - \frac{6x^3}{3} - 8x = \frac{8x^5}{5} + x^4 - 2x^3 - 8x + C$

S)  $\int (2 + 3x^2 - 8x^3) dx$  ← Directo  
 $2x + \frac{3x^3}{3} - \frac{8x^4}{4} = 2x + x^3 - 2x^4 + C$

T)  $\int \sqrt[3]{x} (x+1) dx$   
 $x^{\frac{1}{3}}(x+1) = x^{\frac{4}{3}} + x^{\frac{1}{3}}$   
 $\frac{x^{\frac{4}{3} + \frac{3}{3}}}{\frac{4}{3} + \frac{3}{3}} = \frac{x^{\frac{7}{3}}}{\frac{7}{3}} = \frac{3x^{\frac{7}{3}}}{7}$   
 $\frac{x^{\frac{1}{3} + \frac{3}{3}}}{\frac{1}{3} + \frac{3}{3}} = \frac{x^{\frac{4}{3}}}{\frac{4}{3}} = \frac{3x^{\frac{4}{3}}}{4}$   
 $\frac{3x^{\frac{7}{3}}}{7} + \frac{3x^{\frac{4}{3}}}{4} + C$

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U)  $\int (ax^2 + bx + c) dx$  ← Directo  
 $\frac{ax^3}{3} + \frac{bx^2}{2} + cx + C$

V)  $\int (\sqrt{x} - \frac{1}{\sqrt{x}}) dx$   
 $x^{\frac{1}{2}} - \frac{1}{x^{\frac{1}{2}}}$   
 $\frac{x^{\frac{1}{2} + \frac{1}{2}}}{\frac{1}{2} + \frac{1}{2}} = \frac{x^1}{1} = x$   
 $-\frac{x^{-\frac{1}{2} + \frac{1}{2}}}{-\frac{1}{2} + \frac{1}{2}} = \frac{x^0}{0} = \frac{x^{\frac{1}{2}}}{\frac{1}{2}} = 2x^{\frac{1}{2}}$   
 $\frac{2x^{\frac{3}{2}}}{3} - 2x^{\frac{1}{2}} + C$

