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$$\begin{aligned} 2 \int \sin 3x \sin 2x dx &= \int \frac{1}{2} [\cos(3x-2x) - \cos(3x+2x)] dx \\ &= \frac{1}{2} \int \cos x dx - \frac{1}{2} \int \cos 5x dx = \frac{1}{2} \sin x - \frac{1}{2} \cdot \frac{1}{5} \sin 5x + c \\ &= \boxed{\frac{1}{2} \sin x - \frac{1}{10} \sin 5x + c} \end{aligned}$$

$$\begin{aligned} 3 \int \sin 3x \cos 5x dx &= \int \frac{1}{2} [\sin(3x-5x) + \sin(3x+5x)] dx \\ &= \frac{1}{2} \int \sin(-2x) dx + \frac{1}{2} \int \sin 8x dx = \frac{1}{2} \cdot \frac{1}{2} \cos(-2x) + \frac{1}{2} \cdot \frac{1}{8} \cos 8x + c \\ &= \boxed{\frac{1}{4} \cos(-2x) + \frac{1}{16} \cos 8x + c} \end{aligned}$$

$$\begin{aligned} 4 \int \cos 4x \cos 2x dx &= \int \frac{1}{2} [\cos(4x-2x) + \cos(4x+2x)] dx \\ &= \frac{1}{2} \int \cos 2x dx + \frac{1}{2} \int \cos 6x dx = \frac{1}{2} \cdot \frac{1}{2} \sin 2x + \frac{1}{2} \cdot \frac{1}{6} \sin 6x + c \\ &= \boxed{\frac{1}{4} \sin 2x + \frac{1}{12} \sin 6x + c} \end{aligned}$$

$$\begin{aligned} 5 \int \sqrt{1-\cos x} dx &= \int \sqrt{2 \sin^2 \frac{x}{2}} dx = 2 \int \left| \sin \frac{x}{2} \right| dx = \\ &= 2 \int \sin \frac{x}{2} dx = \boxed{-2x \cos \frac{x}{2} + c.} \end{aligned}$$