



**NOMBRE: RUBI DE JESUS ALVAREZ SANCHEZ**  
**MATERIA: MATEMATICA APLICADA (EXAMEN)**  
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**6TO SEMESTRE ENFERMERIA**

Examen  
Rubí De Jesús Álvarez Sánchez.

$$\begin{aligned} 1. \int \sin^{-1} 3x^2 dx &= \\ &= \sqrt{1-(3)(x^2)} + x^2 \sin^{-1}(3x^2) + c \\ &= \frac{\sqrt{1-9x^4} + x^2}{3 \operatorname{Sen} 3x^2} \\ &= \sqrt{1/3 - 3x^4} + \frac{x^2}{\operatorname{Sen} 3x^2} + c \end{aligned}$$

$$\begin{aligned} 2. \int \cos^{-1} 5x dx &= \\ &= x \cos^{-1}(5x) - \frac{\sqrt{1-(5x)^2}(x)}{5} + c \\ &= \frac{x}{\cos 5x} - \frac{\sqrt{1-25x^2}}{5} + c \\ &= \frac{x}{\cos 5x} - \sqrt{1/5 - 25x^2} + c \end{aligned}$$

$$\begin{aligned} 3. \int \tan^{-1} 1/x^2 dx &= \\ &= x^2 \tan^{-1}(1/x^2) - \frac{\ln|(1)^2(x^2)^2 + 1}{2(1)} + c \\ &= \frac{x^2}{\tan 1/x^2} - \frac{\ln|1x^4 + 1}{2} + c \end{aligned}$$

$$\begin{aligned}
 4. & \int \cos^3 2x / 3 \, dx \\
 &= \frac{1}{3} \int \cos^2 \frac{2x}{3} \cdot \cos 2x \, dx = \frac{1}{3} \int \frac{\cos^2 2x}{3} \cdot \cos 2x \, dx \\
 &= \frac{1}{3} \int \cos^3 2x \, dx = u = 2x = \frac{1}{3} \int \cos^3 \frac{1}{2} u^3 \, du = \frac{1}{3} - \frac{1}{2} \\
 & \int \cos^3 \frac{1}{2} u \, du = \frac{1}{3} \cdot \frac{1}{2} \int \cos u \cos^2 u \, du \\
 &= \frac{1}{6} (\sin 2x - \sin \frac{3 \cdot 2}{3} x) + C
 \end{aligned}$$

$$\begin{aligned}
 5. & \int \sec^4 2x \, dx = \sec^2 u \, du = \tan^2 u + 1 \\
 &= \sec^2 2x \sec^2 2x \, dx \\
 &= \int (\tan^2 2x + 1) \sec^2 2x \, dx
 \end{aligned}$$

$$= \int \tan^2 2x \sec^2 2x \, dx + \int \sec^2 2x \, dx \rightarrow \int \sec^2 v \, dv = \tan v$$

$$\begin{aligned}
 v &= \tan 2x \\
 dv &= 2 \sec^2 2x \, dx \\
 \frac{dv}{2} &= \sec^2 2x \, dx
 \end{aligned}$$

$$\begin{aligned}
 v &= 2x \\
 dv &= 2 \, dx \\
 \frac{dv}{2} &= dx
 \end{aligned}$$

$$\begin{aligned}
 &= \int v^2 \, dv + \int \sec^2 v \, dv = \frac{1}{2} \int v^2 \, dv + \frac{1}{2} \int \sec^2 v \, dv \\
 &= \frac{1}{2} \left( \frac{v^3}{3} \right) + \frac{1}{2} \tan v + C = \frac{1}{6} v^3 + \frac{1}{2} \tan v + C \\
 &= \frac{1}{6} \tan^3 2x + \frac{1}{2} \tan 2x + C
 \end{aligned}$$



$$6. \int \csc^{-1} 2x^2 dx =$$

$$= \ln \left| \frac{2\sqrt{(2)^2 (x^2)^2 - 2} + (2x^2) + x^2 (2x^3)}{2} \right| + C$$

$$= \ln \left| \frac{\sqrt{4x^4} + 2x^2 + x^2}{2} \right| + C$$

$$\frac{\csc^{-1} 2x^2}{2} + \ln \left| \frac{\sqrt{2x^2 - 1} + x^2}{\csc 2x^2} \right| + C$$

$$7. \int \cot^{-1} \sqrt{2} x dx = \ln \left| \frac{\sqrt{2} \sqrt{x^2 + 1} + x}{x \cot^{-1}(\sqrt{2}x)} \right| + C$$

$$= \frac{\ln |2x^2 + 1|}{2.82} + \frac{x}{\cot + \sqrt{2}x} + C$$

$$8. \int \sec^{-1} \sqrt{2} x^2 dx$$

$$= \frac{\sqrt{1 - (\sqrt{2})^2 x^2} (x^2)^2 + x^2 \sec^{-1}(\sqrt{2}x^2)}{\sqrt{2}} + C$$

$$\frac{\sqrt{1 - 2x^4}}{1.41} + \frac{x^2}{\sec \sqrt{2}x^2} + C$$

$$9. \int \sinh^{-1} \frac{1}{x^2} dx$$

$$y = \sinh^{-1} \left( \frac{x}{2} \right) + \frac{x^{1/2}}{\sqrt{1 + (x/c)^2}} = \frac{2x}{2\sqrt{6x^2}} = \sinh^{-1} \left( \frac{x}{2} \right)$$

$$+ \frac{x}{6x^2} - \frac{x}{\sqrt{6x^2}} = \sinh^{-1} \left( \frac{x}{2} \right)$$

$$\begin{aligned}
 10. \int \sinh 2x \, dx &= \int \frac{(e^x - e^{-x})}{2} \, dx \\
 &= \frac{\int (e^x - e^{-x})^2 \, dx}{4} - \frac{1}{4} \int (e^x)^2 - 2 + (e^{-x})^2 \, dx \\
 &= \frac{1}{4} \int (e^{2x} - 2 + e^{-2x}) \, dx \\
 &= \frac{1}{4} \left( \frac{1}{2} e^{2x} - 2x - \frac{1}{2} e^{-2x} \right) + C \\
 &= -\frac{1}{2} x + \frac{1}{4} \frac{(e^{2x} - e^{-2x})}{2} + C
 \end{aligned}$$