

INTEGRACIONES Viridiana Merida Ortiz

$$1) \int x^n dx = \frac{x^{n+1}}{n+1} + c$$

$$\int x^4 dx = \frac{x^{4+1}}{4+1} + c$$

$$\int x^4 dx = \frac{x^5}{5} + c = \frac{1}{5} x^5 + c$$

$$2) \int k \cdot f(x) dx = k \cdot \int f(x) dx$$

$$3 \int x^2 dx = 3 \cdot \frac{x^{2+1}}{2+1} + c$$

$$3 \int x^2 dx = 3 \cdot \frac{x^3}{3} + c = x^3 + c$$

$$3) \int (3x^2 + 2x + 6x^3 + 1) dx = \int [f(x) \pm g(x)] dx = \int f(x) dx \pm \int g(x) dx$$

$$= \int 3x^2 dx + \int 2x dx + \int 6x^3 dx + \int 1 dx$$

$$= 3 \int x^2 dx + 2 \int x dx + 6 \int x^3 dx + \int 1 dx$$

$$= \frac{3x^{2+1}}{2+1} + \frac{2x^{1+1}}{1+1} + \frac{6x^{3+1}}{3+1} + \frac{x^{1+1}}{1+1} + c$$

$$= \frac{3x^3}{3} + \frac{2x^2}{2} + \frac{6x^4}{4} + \frac{x^2}{2} + c$$

$$= x^3 + x^2 + \frac{6}{4}x^4 + \frac{x^2}{2} + c$$

$$4) \int \frac{2x^2 + 3x^4 + x + 5}{x} dx = \int [f(x) \pm g(x)] dx = \int f(x) dx + \int g(x) dx$$

$$= \int \frac{2x^2}{x} dx + \int \frac{3x^4}{x} dx + \int \frac{x}{x} dx + \int \frac{5}{x} dx$$

$$= 2 \int x dx + 3 \int x^3 dx + \int dx + 5 \int \frac{dx}{x}$$

$$= \frac{2x^2}{2} + \frac{2x^4}{4} + x + 5 \cdot \ln|x| + c$$

$$= x^2 + \frac{2}{4}x^4 + x + 5 \cdot \ln|x| + c$$

5) $\int \sqrt{x} \cdot (x + 3) dx$
 $= \int x \cdot \sqrt{x} dx + \int 3\sqrt{x} dx$
 $= \int x \cdot x^{1/2} dx + \frac{3x^{1/2}}{x} dx$
 $= \int x^{3/2} dx + \int 3x^{-1/2} dx$
 $= \frac{x^{3/2+1}}{3/2+1} + 3 \int x^{-1/2} dx = \frac{x^{5/2}}{5/2} + \frac{3x^{-1/2+1}}{-1/2+1} + C$
 $= \frac{2x^{5/2}}{5} + \frac{3x^{1/2}}{1/2} + C$
 $= \frac{2}{5}x^{5/2} + 6x^{1/2} + C = \frac{2}{5}\sqrt{x^5} + 6\sqrt{x} + C$

6) $\int (x^{3/5} - x) dx$
 $= \int x^{3/5} dx - \int x dx$
 $= \frac{x^{3/5+1}}{3/5+1} - \frac{x^{1+1}}{1+1} + C = \frac{x^{8/5}}{8/5} - \frac{x^2}{2} + C$
 $= \frac{5}{8}x^{8/5} - \frac{1}{2}x^2 + C$

7) $\int \frac{5}{x^2} dx$
 $= 5 \int \frac{1}{x^2} dx = 5 \int x^{-2} dx = 5 \frac{x^{-2+1}}{-2+1} + C$
 $= \frac{5x^{-1}}{-1} + C = -\frac{5}{x} + C$

8) $\int \frac{x^3 + 2}{x} dx$
 $= \int \frac{x^3}{x} dx + \int \frac{2}{x} dx = \int x^2 dx + 2 \int \frac{dx}{x}$
 $= \frac{x^{2+1}}{2+1} + 2 \cdot \ln|x| + C$
 $= \frac{1}{3}x^3 + 2 \ln|x| + C$



$$\begin{aligned} 9) & \int (2x^5 + 6x + 3x^2) dx \\ &= \int 2x^5 dx + \int 6x dx + \int 3x^2 dx \\ &= 2 \int x^5 dx + 6 \int x dx + 3 \int x^2 dx \\ &= \frac{2x^{5+1}}{5+1} + \frac{6x^{1+1}}{1+1} + \frac{3x^{2+1}}{2+1} = \frac{2x^6}{6} + \frac{6x^2}{2} + \frac{3x^3}{3} \\ &= \frac{2}{6}x^6 + 3x^2 + x^3 \end{aligned}$$

$$\begin{aligned} 10) & \int \frac{3\sqrt{x^2} + \sqrt{x} + x}{x} dx = \\ &= \int \frac{3\sqrt{x^2}}{x} dx + \int \frac{\sqrt{x}}{x} dx + \int \frac{x}{x} dx \\ &= \int \frac{x^{2/3}}{x} dx + \int \frac{x^{1/2}}{x} dx + \int dx = \int x^{2/3-1} dx + \int x^{1/2-1} dx + \int dx \\ &= \int x^{-1/3} dx + \int x^{-1/2} dx + \int dx \\ &= \frac{x^{-1/3+1}}{-1/3+1} + \frac{x^{-1/2+1}}{-1/2+1} + x + C \\ &= \frac{x^{2/3}}{2/3} + \frac{x^{1/2}}{1/2} + x + C \\ &= \frac{3}{2}x^{2/3} + 2x^{1/2} + x + C \end{aligned}$$